## All India Aakash Test Series for JEE (Advanced)-2020 <br> TEST - 2A (Paper-2) - Code-E

## Test Date : 24/11/2019

## ANSWERS

| ANSWERS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PHYSICS |  | CHEMISTRY |  | MATHEMATICS |  |
| 1. | (B, D) | 21. | (B, C, D) | 41. | (B, C) |
| 2. | (B, D) | 22. | (A, C, D) | 42. | (B, D) |
| 3. | (A, D) | 23. | (D) | 43. | (A) |
| 4. | (B, C) | 24. | (A, C, D) | 44. | (A, B) |
| 5. | (A) | 25. | (C, D) | 45. | (B, C) |
| 6. | (D) | 26. | (D) | 46. | (C) |
| 7. | (B) | 27. | (B) | 47. | (D) |
| 8. | (C) | 28. | (A) | 48. | (A) |
| 9. | (A) |  | (B) | 49. | (D) |
| 10. | (C) | 30. | (A) | 50. | (A) |
| 11. | (C) | 31. | (B) | 51. | (C) |
| 12. | (B) | 32. | (A) | 52. | (D) |
| 13. | (C) |  | (B) | 53. | (B) |
| 14. | (B) | 34. | (C) | 54. | (A) |
| 15. | (A) | 35. | (A) | 55. | (C) |
| 16. | $A \rightarrow(P, R)$ | 36. | $A \rightarrow(Q, S)$ | 56. | $\mathrm{A} \rightarrow$ (P) |
|  | $B \rightarrow(P, S)$ |  | $B \rightarrow(R)$ |  | $B \rightarrow(Q)$ |
|  | $\mathrm{C} \rightarrow(\mathrm{Q}, \mathrm{T})$ |  | $\mathrm{C} \rightarrow(\mathrm{Q}, \mathrm{R})$ |  | $\mathrm{C} \rightarrow(\mathrm{Q}, \mathrm{S})$ |
|  | $D \rightarrow(Q, S)$ |  | $\mathrm{D} \rightarrow(\mathrm{P}, \mathrm{T})$ |  | $\mathrm{D} \rightarrow(\mathrm{R}, \mathrm{S})$ |
| 17. | $A \rightarrow(R, T)$ | 37. | $\mathrm{A} \rightarrow(\mathrm{Q}, \mathrm{S})$ | 57. | $A \rightarrow(P, Q)$ |
|  | $B \rightarrow(S, T)$ |  | $B \rightarrow(Q)$ |  | $B \rightarrow(P, Q)$ |
|  | $\mathrm{C} \rightarrow(\mathrm{Q}, \mathrm{S})$ |  | $\mathrm{C} \rightarrow(\mathrm{R}, \mathrm{T})$ |  | $C \rightarrow(R, T)$ |
|  | $\mathrm{D} \rightarrow(\mathrm{Q}, \mathrm{S})$ |  | $\mathrm{D} \rightarrow(\mathrm{Q})$ |  | $\mathrm{D} \rightarrow(\mathrm{S}, \mathrm{T})$ |
| 18. | (02) | 38. | (07) | 58. | (09) |
| 19. | (01) |  | (03) | 59. | (00) |
| 20. | (06) | 40. | (06) | 60. | (03) |

## HINTS \& SOLUTIONS

## PART - I (PHYSICS)

1. Answer (B, D)

Hint : $B$ and $C$ will be in series.
Solution :

$$
\begin{aligned}
& C_{B C}=\frac{2 \times 3}{2+3}=\frac{6}{5} \mu \mathrm{~F} \\
& \therefore \quad \Delta q_{S}=\frac{\frac{6}{5}}{\frac{6}{5}+1} \times 110=60 \mu \mathrm{C} \\
& \therefore \quad q_{A}=110-60=50 \mu \mathrm{C} \\
& \quad V_{B}=\frac{60}{2}=30 \mathrm{~V}, V_{C}=\frac{60}{3}=20 \mathrm{~V}
\end{aligned}
$$

2. Answer (B, D)

Hint : Particle performs SHM.

## Solution :

$$
\begin{aligned}
& E=\frac{Q x}{4 \pi \varepsilon_{0}\left(R^{2}+x^{2}\right)^{\frac{3}{2}}}, x \ll R \\
& \Rightarrow \quad E=\frac{Q x}{4 \pi \varepsilon_{0} R^{3}} \\
& \therefore \quad \omega=\sqrt{\frac{Q q}{m \times 4 \pi \varepsilon_{0} R^{3}}} \\
& \therefore \quad T=2 \pi \sqrt{\frac{m \times 4 \pi \varepsilon_{0} R^{3}}{Q q}}=4 \pi \sqrt{\frac{\pi \varepsilon_{0} m R^{3}}{Q q}}
\end{aligned}
$$

and, $V_{\max }=\omega a=\frac{a x}{2} \sqrt{\frac{Q q}{\pi \varepsilon_{0} m R^{3}}}$
3. Answer (A, D)

Hint : Frequency as well as wavelength change.

## Solution :

$\lambda_{1}=\lambda_{0}-\frac{V}{5} T \Rightarrow \lambda_{1}=\frac{4 \lambda_{0}}{5}$
$\therefore \quad \lambda_{2}=2 \lambda_{1}=\frac{8 \lambda_{0}}{5}$
and, $T^{\prime}=\frac{\lambda^{\prime}}{2 V+\frac{V}{5}}=\frac{5 \lambda^{\prime}}{11 V}$
$\therefore \quad f^{\prime}=\frac{1}{T^{\prime}}=\frac{11 \mathrm{~V}}{5 \times\left(\frac{8 \lambda_{0}}{5}\right)}=\frac{11 \mathrm{~V}}{8 f_{0}}$
4. Answer (B, C)

Hint: $\Delta Q=\Delta U+\Delta W$

## Solution :

$$
\begin{aligned}
& Q=\Delta U+\frac{Q}{2} \Rightarrow \Delta U=\frac{Q}{2} \\
& \Rightarrow \quad n \times\left(\frac{3 R}{2}\right) \cdot \Delta T=\frac{n C \Delta T}{2} \\
& \Rightarrow C=3 R \\
& \text { And, } \Delta U=\Delta W \\
& \Rightarrow \quad n\left(\frac{3 R}{2}\right) \cdot d T=P d V \\
& \Rightarrow \quad P^{3} V=\text { constant } \\
& \Rightarrow \quad P^{2} \times T=\text { constant } \\
& \Rightarrow P \propto \frac{1}{\sqrt{T}}
\end{aligned}
$$

5. Answer (A)

Hint : A balanced wheatstone bridge is formed.

## Solution :

$\therefore \quad V_{D}-V_{C}=0$
$\therefore \quad R_{\text {eq }}=\frac{12 \times 6}{12+6}=4 \Omega$
$\therefore \quad I_{\text {battery }}=\frac{20}{4}=5 \mathrm{~A}$
$I_{A D}=\frac{20}{12}=\frac{5}{3} \mathrm{~A}$
6. Answer (D)

Hint : Two spheres behave as capacitor and then become in parallel finally.

## Solution :

$$
\begin{aligned}
& Q_{0}=4 \pi \varepsilon_{0}(2 a) \times V \\
& \begin{aligned}
\therefore \quad i=\frac{V}{R} e^{-\frac{t}{\tau}}, \quad \tau & =R \times\left(\frac{C_{1} C_{2}}{C_{1}+C_{2}}\right) \\
& =R \times \frac{4 \pi \varepsilon_{0} a \times 2 a}{3 a} \\
& =\frac{8 \pi \varepsilon_{0} R a}{3} \\
\therefore \quad i & =\frac{V}{R} e^{-\frac{3 t}{8 \pi \varepsilon_{0} R a}}
\end{aligned}
\end{aligned}
$$

7. Answer (B)

Hint : Two spheres behave as capacitor and then become in parallel finally.

## Solution :

Final charge on smaller sphere

$$
\begin{aligned}
q_{2} & =\frac{C_{2}}{C_{1}+C_{2}} \times Q_{0} \\
& =\frac{4 \pi \varepsilon_{0} \times a}{4 \pi \varepsilon_{0}(a+2 a)} \times\left[4 \pi \varepsilon_{0} \times(2 a) \times V\right] \\
& =\frac{1}{3} \times 8 \pi \varepsilon_{0} a V
\end{aligned}
$$

8. Answer (C)

Hint : Two spheres behave as capacitor and then become in parallel finally.

## Solution :

Total heat dissipation

$$
\begin{aligned}
H & =\frac{1}{2} \times\left(\frac{C_{1} C_{2}}{C_{1}+C_{2}}\right) \times V^{2} \\
& =\frac{1}{2} \times \frac{2}{3} \times\left(4 \pi \varepsilon_{0} a\right) V^{2} \\
& =\frac{4 \pi \varepsilon_{0} a V^{2}}{3}
\end{aligned}
$$

9. Answer (A)

Hint : Speed of sound, $V=\sqrt{\frac{\gamma R T}{M}}$

## Solution :

$V=\sqrt{\frac{\gamma R T}{M}}$
$\Rightarrow \quad T=\frac{V^{2} M}{\gamma R}=\frac{(300)^{2} \times\left(29 \times 10^{-3}\right)}{1.4 \times 8.314}$

$$
\simeq 224 \mathrm{~K}
$$

10. Answer (C)

Hint : Put the value of $T_{0}$.

## Solution :

$\because \quad T=T_{0}-0.006 h_{0}$
$\Rightarrow 273=224-0.006 \times h_{0}$
$\Rightarrow h_{0}=8170 \mathrm{~m}$
11. Answer (C)

Hint: Put the value of $h_{0}$.

## Solution :

$$
\begin{aligned}
P & =P_{0}\left(1-\frac{0.006 \times 8170}{273}\right) \frac{29 \times 10^{-3} \times 9.8}{8.31 \times 0.006} \\
& =P_{0} \times(0.82)^{5.7} \\
& =0.32 P_{0}
\end{aligned}
$$

12. Answer (B)

Hint : Use KVL and KCL

## Solution :

For $R_{A B}$

$\therefore \quad R_{A B}=\frac{7 R}{12}$
For $R_{A C}$

$\therefore \quad R_{A C}=\frac{3 R}{4}$
$\therefore \quad \frac{R_{A B}}{R_{A C}}=\frac{7 \times 4}{12 \times 3}=\frac{7}{9}$

## 13. Answer (C)

Hint: Flux $=\frac{q}{4 \pi \varepsilon_{0}} \times$ Solid angle $\times 2$

## Solution :

$$
\begin{aligned}
\phi & =\frac{q}{\varepsilon_{0}} \times \frac{2 \pi(1-\cos \theta)}{4 \pi} \times 2 \\
& =\frac{q}{\varepsilon_{0}}\left(1-\frac{\ell}{\sqrt{\ell^{2}+R^{2}}}\right) \\
& =\frac{q}{\varepsilon_{0}}\left(1-\frac{2}{\sqrt{5}}\right)
\end{aligned}
$$

14. Answer (B)

Hint : Use concept of standing wave.

## Solution :

$y=y_{1}+y_{2}$

$$
\begin{aligned}
& =a\left[\sin \left(\frac{\pi}{2} x-\omega t\right)+\sin \left(\frac{\pi}{2} x+\omega t+\frac{\pi}{3}\right)\right] \\
\Rightarrow \quad y & =2 a \sin \left(\frac{\pi}{2} x+\frac{\pi}{6}\right) \cdot \cos \left(\cot +\frac{\pi}{6}\right)
\end{aligned}
$$

For nodes, $2 a \sin \left(\frac{\pi}{2} x+\frac{\pi}{6}\right)=0$
$\Rightarrow \quad \frac{\pi}{2} x+\frac{\pi}{6}=\pi, 2 \pi, 3 \pi, 4 \pi, \ldots$.
$\Rightarrow \quad x=\frac{5}{3}, \frac{11}{3}, \frac{17}{3}, \frac{23}{3}$
$\therefore$ For $0 \leq x \leq 6$,
Number of nodes $=3$
15. Answer (A)

Hint: $P^{1-\gamma} T^{\gamma}=$ constant

## Solution :

$P_{1}^{1-\gamma} T_{1}^{\gamma}=P_{2}^{1-\gamma} T_{2}^{\gamma}$
$\Rightarrow \quad T_{2}=1000 \times\left(\frac{3}{2}\right)^{\left(\frac{3}{5}-1\right)}=850 \mathrm{~K}$
Then, $\frac{P_{3}}{T_{3}}=\frac{P_{2}}{T_{2}} \Rightarrow T_{3}=425 \mathrm{~K}$

$$
\begin{aligned}
\therefore \quad \Delta Q=n C_{v} \Delta T & =1 \times\left(\frac{3 R}{2}\right) \times(850-425) \\
& =5300 \mathrm{~J}
\end{aligned}
$$

16. Answer $A(P, R) ; B(P, S) ; C(Q, T) ; D(Q, S)$

Hint : After earthing, charge on outer surface of outer most plates becomes zero.

## Solution :

Before earthing


After earthing

$V_{A B}=\frac{Q d}{\varepsilon_{0} A}, V_{B C}=\frac{3 Q d}{\varepsilon_{0} A}, V_{C D}=0, V_{D E}=\frac{3 Q d}{\varepsilon_{0} A}$
17. Answer $A(R, T) ; B(S, T) ; C(Q, S) ; D(Q, S)$

Hint : In isothermal process $\Delta U=0$

## Solution :

For A : PV = constant
$\Rightarrow \Delta U=0, \Delta W=$ positive
$\Rightarrow \Delta Q=$ positive
For $\mathrm{B}: P=\frac{p R T}{m} \Rightarrow T=$ constant
$\Rightarrow \Delta U=0, \Delta W=-$ negative, $\Delta Q=$ negative
And so on.
18. Answer (02)

Hint : Reduce it to a finite circuit.

## Solution :

$R_{A B}=R_{C D}, V_{C D}=\frac{1}{2} V_{A B}$
$\therefore \quad$ Current gets equally distributed
$\therefore \quad R_{2}=R_{A B}$
And, $R_{A B}=R_{1}+\left(\frac{R_{2}}{2}\right)=R_{2}$
$\Rightarrow \frac{R_{2}}{R_{1}}=2$
19. Answer (01)

Hint : Use Newton's law.
Solution :

$$
\begin{aligned}
& \frac{-d T}{d t}=b\left(T-T_{s}\right) \\
& \Rightarrow \quad \Delta T=(\Delta T)_{0} e^{-b t} \\
& \therefore \quad t_{2}=2 t_{0} \\
& \therefore \quad n=1
\end{aligned}
$$

20. Answer (06)

Hint : Use superposition principle.
Solution :
$E_{1}=\frac{Q}{4 \pi \varepsilon_{0} a^{2}}$

$\therefore \quad E_{\text {net }}=3 \times\left(E_{1} \cos \theta\right)=3 \times \frac{Q}{4 \pi \varepsilon_{0} a^{2}} \times \sqrt{\frac{2}{3}}$

$$
=\frac{Q \sqrt{6}}{4 \pi \varepsilon_{0} a^{2}}
$$

## PART - II (CHEMISTRY)

21. Answer (B, C, D)

Hint : Benzaldehyde is not oxidised by Fehling's reagent.
Solution :
Acetophenone can give iodoform and bromoform.
22. Answer (A, C, D)

Hint :


2. $\begin{aligned} & \text { 2. } \mathrm{NI} \\ & \text { 2 }\end{aligned}$

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Solution :
$Q$ is

26. Answer (D)

Hint : Given D-glyceraldehyde is 'R'


## Solution :



$R$ as well as $D$.
27. Answer (B)

Hint : D and L convention is used for amino acids also

Solution :
(D) fructose is laevorotatory (I)
(D) glucose is dextrorotatory(d)
28. Answer (A)

Hint : Product obtained after ozonolysis



Solution :
$C^{*}$ is $L$
$C^{\#}$ is $D$.
29. Answer (B)
30. Answer (A)
31. Answer (B)

Hint and Solution : Q. Nos. 29 to 31

(B)


## Solution :



$\mathrm{CH}_{2} \mathrm{O}$ (excess)
32. Answer (A)

Hint : It is electrophilic substitution reaction.

## Solution :

The intermediate formed when ${ }^{+} \mathrm{NO}_{2}$ attacks at position C-2 is more stable.
33. Answer (B)

Hint :


## Solution :


34. Answer (C)

Hint :


Solution :

35. Answer (A)

Hint : Excess of ether and water as solvent will favour $S_{N} 1$ reaction.

## Solution :


36. Answer A(Q, S); B(R); C(Q, R); D(P, T)

Hint :


## Solution :



37. Answer $A(Q, S) ; B(Q) ; C(R, T) ; D(Q)$

Hint : $\mathrm{LiAlH}_{4}$ is a very strong reducing agent can reduce almost functional groups to lower oxidation state, except alkenes and alkynes.

## Solution :

$\mathrm{NaBH}_{4}$ cannot reduce amide into amine
$\mathrm{NaBH}_{4}$ can reduce only acid halide into alcohol among the given transformation.
38. Answer (07)

Hint :


## Solution :

$x=1, y=2, z=4$
39. Answer (03)

Hint :


## Solution :



Possible Products
40. Answer (06)

Hint: O, P-substituted Bromo group are more likely to get substituted.

## Solution :

The Br group at position 4 is most likely to get substitute and at position 2 , is least

## PART - III (MATHEMATICS)

41. Answer (B, C)

Hint : Translation and Rotation of axes.

## Solution :

For $f(x, y)=0$
new origin=
$\left(\frac{h f-b h}{a b-h^{2}}, \frac{g f-a f}{a b-h^{2}}\right) \equiv\left(\frac{28}{-14}, \frac{42}{-14}\right) \equiv(-2,-3)$
For $g(x, y)=0$
$\theta=\frac{1}{2} \tan ^{-1}\left(\frac{2 h}{a-b}\right)=\frac{1}{2} \tan ^{-1}\left(\frac{2 \times \sqrt{3}}{2}\right)$
$=\frac{1}{2} \times \frac{\pi}{3}=\frac{\pi}{6}$
42. Answer (B, D)

Hint : Distance between two parallel lines.

## Solution :

Distance between two parallel lines $=2 \sqrt{5}$
$\therefore$ points on line $\frac{x-1}{-2}=\frac{y+2}{1}= \pm 2 \sqrt{5}$

$$
\overline{\sqrt{5}} \quad \overline{\sqrt{5}}
$$

$\therefore$ points are $(-3,0)$ and $(5,-4)$
$\therefore$ Required lines are

$$
2 x-y+6=0 \text { and } 2 x-y-14=0
$$

43. Answer (A)

Hint : Division formula between two points.

## Solution :

$$
A\left(\frac{a b}{a+b}\left(\frac{1-m}{-m}, 0\right): B\left(-0, \frac{a b}{a+b}(1-m)\right)\right.
$$

Mid-point of $A B$ is $(h, k)$
$\therefore 2 h=\frac{a b}{a+b} \frac{(m-1)}{m} ; 2 k \frac{a b}{a+b}(1-m)$
$\therefore \frac{1}{2 h}+\frac{1}{2 k}=\frac{a+b}{a b}$
$\Rightarrow \mathrm{ab}(x+y)=2(a+b) x y$ is the locus

Let $P$ divides $A B$ in ratio $1: 3$
$\therefore P\left(\frac{\frac{3 a b}{a+b}\left(1-\frac{1}{m}\right)}{4}, \frac{\frac{a b}{a+b}(1-m)}{4}\right)$
$\therefore(x+3 y) a b \equiv 4(a+b) x y$ is the required locus
44. Answer (A, B)

Hint : Condition of two degree equation (to represent pair of straight line.

## Solution :

$\Delta=0 \Rightarrow a b c+2 f g h=a f^{2}+b g^{2}+c h^{2}$
$\Rightarrow c=\frac{-10}{9}$
Also
$\cos \alpha=\left|\frac{a+b}{\sqrt{(a-b)^{2}+4 h^{2}}}\right| \Rightarrow \alpha=\cos ^{-1}\left(\frac{5}{\sqrt{34}}\right)$
45. Answer (B, C)

Hint : Perpendicularity of two lines.

## Solution :

$L_{1}$ and $L_{2}$ if they are $\perp$ to a common line $\Rightarrow \lambda=-1$ for two adjacent sides of a square
$L_{1} \perp L_{2}$
$\therefore\left(\lambda^{2}+1\right) \lambda^{2}=1$
$\Rightarrow \lambda^{5}+2 \lambda^{3}+\lambda-1=0=f(\lambda)$
$\therefore f^{\prime}(\lambda)=5 \lambda^{4}+6 \lambda^{2}+1=0$
$\therefore f(\lambda)=0$ has only one real root
46. Answer (C)

Hint : Family of circle with line.

## Solution :

Let required circle
$x^{2}+y^{2}-3 x+2 y-4+\lambda(2 x+5 y+2)=0$
$\therefore C\left(\frac{3-2 \lambda}{2}, \frac{-(5 \lambda+2)}{2}\right)$ satisfy $x+y=11$
$\therefore \lambda=-3$
$\therefore$ Required circle is $x^{2}+y^{2}-9 x-13 y-10=0$
47. Answer (D)

Hint : Orthogonal of two circles.

## Solution :

Let required circle
$(x-1)^{2}+(y+1)^{2}+\lambda(2 x+3 y+1)=0$
Circle with diameter points $(0,3)$ and $(-2,-1)$ is
$x^{2}+y^{2}+2 x-2 y-3=0$
(i) of (ii) intersect orthogonally
$\therefore(2 \lambda-1)+-2\left(\frac{3 \lambda}{2}+1\right)=\lambda-1 \Rightarrow \lambda=\frac{-3}{2}$
Required circle is $2 x^{2}+2 y^{2}-10 x-5 y+1=0$
48. Answer (A)

Hint : Touching concept of line with circle.

## Solution :

Let required circle
$\left(x^{2}+y^{2}-4\right)+\lambda(x+2 y-4)=0$
$C\left(\frac{-\lambda}{2},-\lambda\right)=\lambda=\sqrt{\frac{5 \lambda^{2}}{4}+4 \lambda+4}$
$\because$ it touches line $x+2 y-5=0$

$$
\begin{aligned}
& \therefore\left|\frac{\frac{-\lambda}{2}+2(-\lambda)-5}{\sqrt{5}}\right|=\sqrt{\frac{5 \lambda^{2}}{4}+4 \lambda+4} \\
& \Rightarrow 5(\lambda+2)^{2}=5 \lambda^{2}+16 \lambda+16 \\
& \Rightarrow \lambda=-1
\end{aligned}
$$

$\therefore$ Required circle $x^{2}+y^{2}-x-2 y=0$
49. Answer (D)

Hint : Chord of contact of circle.

## Solution :

Equation of C.O.C $h x+k y=8$
Also $t k=h+2 t^{2}$ (ii) $\because(h, k)$ satisfy tangent)
$\Rightarrow h x+y \frac{\left(h+2 t^{2}\right)}{t}-8=0$
$\Rightarrow 2(t y-4)+h\left(x+\frac{y}{t}\right)=0$
$\therefore \quad$ Line passes through point
$y=\frac{4}{t}$ and $x=\frac{-y}{t}$
$\Rightarrow \frac{y}{4}=-\frac{x}{y} \Rightarrow y^{2}=-4 x$
50. Answer (A)

Hint: Point of intersection of two curves.

## Solution :

Point of intersection of $x=-2$ and $x^{2}+y^{2}=16$
$\therefore y^{2}=12 \Rightarrow y= \pm 2 \sqrt{3}$
$\therefore$ Point $(-2,2 \sqrt{3})$
51. Answer (C)

Hint : Circumcircle of triangle $A B C$

## Solution :

The equation of the circumcircle of $\triangle A Q B$ is
$\left(x^{2}+y^{2}-8\right)+\lambda(h x+k y-8)=0 \because(\mathrm{~A}=-1)$ due to $(0,0)$ satisfy it
$\therefore$ Equation is $x^{2}+y^{2}-h x-k y=0$
Now centre $\left(\frac{h}{2}, \frac{k}{2}\right)$
$\therefore$ For locus let $x=\frac{h}{2} ; y=\frac{k}{2}$
$h=2 x$ and $k=2 y$
$\because t k=h+2 t^{2} \therefore$ at $t=2$
The required locus is $2 y=x+4$
52. Answer (D)

Hint : Length of latus rectum independency.

## Solution :


$\theta=2 \tan ^{-1} 2$
$\because \sqrt{3}<2<\sqrt{2}+1$
$\frac{\pi}{3}<\tan ^{-1} 2<\frac{3 \pi}{8}$
$\Rightarrow \frac{2 \pi}{3}<\theta<\frac{3 \pi}{-4}$
53. Answer (B)

Hint : Condition of common tangent on two curves.

## Solution :

$y=\frac{x}{2}+2$ is tangent on $\frac{x^{2}}{4}+\frac{y^{2}}{b^{2}}=1$
$\Rightarrow 4+4 b^{2}=16 \Rightarrow b^{2}+1=4 \Rightarrow b= \pm \sqrt{3}$
Now tangent at other point is given by $-2 y=x+4$
$\Rightarrow x+2 y+4=0$
54. Answer (A)

Hint : Locus of midpoint of Parallel chords.

## Solution :

Let middle point is $(h, k)$
$\therefore \quad$ Equation of chord in mid-point form is
$\frac{x}{h}+\frac{y}{k}=2$
$\therefore-\frac{1}{h \times \frac{1}{k}}=m \Rightarrow k=-m h$
$\Rightarrow y+m x=0$ is the required locus
55. Answer (C)

Hint : I.T.F. conversion in domain.

## Solution :

Let $\sin ^{-1} x=\theta \Rightarrow x=\sin \theta$
Now

$$
\begin{aligned}
& \cos ^{-1} x=\cos ^{-1}(\sin \theta)=\cos ^{-1}\left(-\cos \left(\frac{3 \pi}{2}-\theta\right)\right) \\
& =\pi-\cos ^{-1}\left(\cos \left(\frac{3 \pi}{2}-\theta\right)\right) \\
& =\pi-\left(\frac{3 \pi}{2}-\theta\right) \text { as } \frac{3 \pi}{2}-\theta \in(0, \pi) \\
& =\theta-\frac{\pi}{2}=\sin ^{-1} x-\frac{\pi}{2} \\
& \therefore \sin ^{-1} x+\cos ^{-1} x=2 \sin ^{-1} x-\frac{\pi}{2}
\end{aligned}
$$

56. Answer $A(P) ; B(Q) ; C(Q, S) ; D(R, S)$

Hint : Type of functions concept.

## Solution :

(A) $f(x)= \begin{cases}\left((1)^{1}\right)^{n} x>0=1 & , x>0 \\ \left((-1)^{-1}\right)^{n} x<0 & , x<0\end{cases}$
$f(x)$ is an odd function. $f(x)$ is not bijective
$\because f(x)$ is not one one
(B) $f(x)=\frac{x}{e^{x}-1}+\frac{x}{2}+1$
$f(x)=\frac{-x}{e^{-x}-1}-\frac{x}{2}+1=x+\frac{x}{e^{x}-1}-\frac{x}{2}+f(x)$
$\therefore f(x)$ is an even function $\because f(x)$ is not bijective
(C) $f(-x)=f(x) \therefore f(x)$ is even. $f(x)$ is periodic but time period not define
(D) $f(x)=\max \{\tan x, \cot x\}$. From graph of $f(x)$ it is clear that
$f(x)$ is neither even nor odd
$\because f(x+\pi)=\max \{\tan (x+\pi), \cot (x+\pi)\}$
$=\max \{\tan x, \cot x\} f(x)$ is periodic with $\mathrm{f}(\mathrm{x})$ is periodic with $\pi$
57. Answer $A(P, Q) ; B(P, Q) ; C(R, T) ; D(S, T)$

Hint : Property of perpendicular normals.

## Solution :

Equation of normal at ' $p$ ' is
$y=-t x+2 a t+a t^{3}$
Put $y=-2 a t \Rightarrow x=4 a+a t^{2}$
$\therefore G\left(4 a+a t^{2},-2 a t\right)$
Required locus $y^{2}=4 a(x-4 a)$

$$
\because a=1
$$

$\therefore y^{2}=4(x-4)$
Now verify each option
58. Answer (09)

Hint : Sum of infinite G.P.

## Solution :

$$
\begin{aligned}
& \frac{1}{1-\sin \left(\cos ^{-1} x\right)}=2 \\
& \Rightarrow \sin \left(\cos ^{-1} x\right)=\frac{1}{2} \\
& \Rightarrow \cos ^{-1} x=\frac{\pi}{6} \Rightarrow x=\frac{\sqrt{3}}{2} \Rightarrow 4 x^{2}=3 \\
& \Rightarrow 12 x^{2}=9
\end{aligned}
$$

59. Answer (00)

Hint : Trigonometric conversion of I.T.F.

## Solution :

$$
\begin{aligned}
& \sin \left(\cos ^{-1}\left(\tan \left(\tan ^{-1}\left(\sqrt{x^{2}-1}\right)\right)\right)\right. \\
& =\sin \left(\cos ^{-1} \sqrt{x^{2}-1}\right) \\
& =\sin \left(\sin ^{-1} \sqrt{2-x^{2}}\right)=\sqrt{2-x^{2}} \\
& \therefore \text { Common domain }[1, \sqrt{2}] \Rightarrow 2-x^{2}=1+x \\
& \Rightarrow x^{2}+x-1=0 \Rightarrow x=\frac{-1 \pm \sqrt{5}}{2} \\
& x=\frac{\sqrt{5}-1}{2} \notin[1, \sqrt{2}]
\end{aligned}
$$

$\therefore$ No solution exists
60. Answer (03)

Hint : Graphical solution.

## Solution :



From graph it is clear that curves intersect at 3 points
$\therefore$ Only 3 solutions

## All India Aakash Test Series for JEE (Advanced)-2020 <br> TEST - 2A (Paper-2) - Code-F

## Test Date : 24/11/2019

## ANSWERS

## PHYSICS

1. $(A)$
2. $(B, C)$
3. $(A, D)$
4. $(B, D)$
5. (B, D)
6. (D)
7. (B)
8. (C)
9. (A)
10. (C)
11. (C)
12. (A)
13. (B)
)
14. (C)
15. (B)
16. $\quad A \rightarrow(R, T)$
$B \rightarrow(S, T)$
$\mathrm{C} \rightarrow(\mathrm{Q}, \mathrm{S})$
$D \rightarrow(Q, S)$
17. $\quad A \rightarrow(P, R)$
$B \rightarrow(P, S)$
$C \rightarrow(Q, T)$
$D \rightarrow(Q, S)$
18. (06)
19. (01)
20. (02)
21. (06)

## CHEMISTRY

21. (C, D)
22. (A, C, D)
23. (D)
24. (A, C, D)
25. $(B, C, D)$
26. (D)
27. (B)
28. (A)
29. (B)
30. (A)
31. (B)
32. (A)
33. (C)
34. (B)
35. (A)
36. $\quad A \rightarrow(Q, S)$
$B \rightarrow(Q)$
$C \rightarrow(R, T)$
$\mathrm{D} \rightarrow(\mathrm{Q})$
37. $\quad A \rightarrow(Q, S)$
$B \rightarrow(R)$
$\mathrm{C} \rightarrow(\mathrm{Q}, \mathrm{R})$
$D \rightarrow(P, T)$
38. (03)
39. (07)
40. (03)

MATHEMATICS
41. $(B, C)$
42. $(A, B)$
43. $(A)$
44. (B, D)
45. (B, C)
46. (C)
47. (D)
48. (A)
49. (D)
50. (A)
51. (C)
52. (C)
53. (A)
54. (B)
55. (D)
56. $\quad A \rightarrow(P, Q)$
$B \rightarrow(P, Q)$
$C \rightarrow(R, T)$
$\mathrm{D} \rightarrow(\mathrm{S}, \mathrm{T})$
57. $\quad A \rightarrow(P)$
$B \rightarrow(Q)$
$C \rightarrow(Q, S)$
$\mathrm{D} \rightarrow(\mathrm{R}, \mathrm{S})$
59. (00)
60. (09)

## HINTS \& SOLUTIONS

## PART - I (PHYSICS)

1. Answer (A)

Hint : A balanced wheatstone bridge is formed.

## Solution :

$\therefore \quad V_{D}-V_{C}=0$
$\therefore \quad R_{\text {eq }}=\frac{12 \times 6}{12+6}=4 \Omega$
$\therefore \quad l_{\text {battery }}=\frac{20}{4}=5 \mathrm{~A}$
$I_{A D}=\frac{20}{12}=\frac{5}{3} \mathrm{~A}$
2. Answer $(B, C)$

Hint: $\Delta Q=\Delta U+\Delta W$

## Solution :

$$
\begin{aligned}
& Q=\Delta U+\frac{Q}{2} \Rightarrow \Delta U=\frac{Q}{2} \\
& \Rightarrow n \times\left(\frac{3 R}{2}\right) \cdot \Delta T=\frac{n C \Delta T}{2} \\
& \Rightarrow C=3 R \\
& \text { And, } \Delta U=\Delta W \\
& \Rightarrow n\left(\frac{3 R}{2}\right) \cdot d T=P d V \\
& \Rightarrow P^{3} V=\text { constant } \\
& \Rightarrow P^{2} \times T=\text { constant } \\
& \Rightarrow P \propto \frac{1}{\sqrt{T}}
\end{aligned}
$$

3. Answer (A, D)

Hint : Frequency as well as wavelength change.
Solution :
$\lambda_{1}=\lambda_{0}-\frac{V}{5} T \Rightarrow \lambda_{1}=\frac{4 \lambda_{0}}{5}$
$\therefore \quad \lambda_{2}=2 \lambda_{1}=\frac{8 \lambda_{0}}{5}$
and, $T^{\prime}=\frac{\lambda^{\prime}}{2 V+\frac{V}{5}}=\frac{5 \lambda^{\prime}}{11 V}$
$\therefore \quad f^{\prime}=\frac{1}{T^{\prime}}=\frac{11 \mathrm{~V}}{5 \times\left(\frac{8 \lambda_{0}}{5}\right)}=\frac{11 \mathrm{~V}}{8 f_{0}}$
4. Answer (B, D)

Hint : Particle performs SHM.

## Solution :

$$
\begin{aligned}
& E=\frac{Q x}{4 \pi \varepsilon_{0}\left(R^{2}+x^{2}\right)^{\frac{3}{2}}}, x \ll R \\
& \Rightarrow \quad E=\frac{Q x}{4 \pi \varepsilon_{0} R^{3}} \\
& \therefore \quad \omega=\sqrt{\frac{Q q}{m \times 4 \pi \varepsilon_{0} R^{3}}} \\
& \therefore \quad T=2 \pi \sqrt{\frac{m \times 4 \pi \varepsilon_{0} R^{3}}{Q q}}=4 \pi \sqrt{\frac{\pi \varepsilon_{0} m R^{3}}{Q q}} \\
& \text { and, } V_{\max }=\omega a=\frac{a x}{2} \sqrt{\frac{Q q}{\pi \varepsilon_{0} m R^{3}}}
\end{aligned}
$$

5. Answer (B, D)

Hint : $B$ and $C$ will be in series.

## Solution :

$$
\begin{aligned}
& C_{B C}=\frac{2 \times 3}{2+3}=\frac{6}{5} \mu \mathrm{~F} \\
& \therefore \quad \Delta q_{S}=\frac{\frac{6}{5}}{\frac{6}{5}+1} \times 110=60 \mu \mathrm{C} \\
& \therefore \quad q_{A}=110-60=50 \mu \mathrm{C} \\
& \quad V_{B}=\frac{60}{2}=30 \mathrm{~V}, V_{C}=\frac{60}{3}=20 \mathrm{~V}
\end{aligned}
$$

6. Answer (D)

Hint : Two spheres behave as capacitor and then become in parallel finally.

## Solution :

$$
\begin{aligned}
& Q_{0}=4 \pi \varepsilon_{0}(2 a) \times V \\
& \therefore \quad i=\frac{V}{R} e^{-\frac{t}{\tau}}, \quad \tau=R \times\left(\frac{C_{1} C_{2}}{C_{1}+C_{2}}\right) \\
& =R \times \frac{4 \pi \varepsilon_{0} a \times 2 a}{3 a} \\
& =\frac{8 \pi \varepsilon_{0} R a}{3} \\
& \therefore \quad i=\frac{V}{R} e^{-\frac{3 t}{8 \pi \varepsilon_{0} R a}}
\end{aligned}
$$

7. Answer (B)

Hint : Two spheres behave as capacitor and then become in parallel finally.

Solution :
Final charge on smaller sphere

$$
\begin{aligned}
q_{2} & =\frac{C_{2}}{C_{1}+C_{2}} \times Q_{0} \\
& =\frac{4 \pi \varepsilon_{0} \times a}{4 \pi \varepsilon_{0}(a+2 a)} \times\left[4 \pi \varepsilon_{0} \times(2 a) \times V\right] \\
& =\frac{1}{3} \times 8 \pi \varepsilon_{0} a V
\end{aligned}
$$

8. Answer (C)

Hint : Two spheres behave as capacitor and then become in parallel finally.

## Solution :

Total heat dissipation

$$
\begin{aligned}
H & =\frac{1}{2} \times\left(\frac{C_{1} C_{2}}{C_{1}+C_{2}}\right) \times V^{2} \\
& =\frac{1}{2} \times \frac{2}{3} \times\left(4 \pi \varepsilon_{0} a\right) V^{2} \\
& =\frac{4 \pi \varepsilon_{0} a V^{2}}{3}
\end{aligned}
$$

9. Answer (A)

Hint : Speed of sound, $V=\sqrt{\frac{\gamma R T}{M}}$

## Solution :

$V=\sqrt{\frac{\gamma R T}{M}}$
$\Rightarrow \quad T=\frac{V^{2} M}{\gamma R}=\frac{(300)^{2} \times\left(29 \times 10^{-3}\right)}{1.4 \times 8.314}$

$$
\simeq 224 \mathrm{~K}
$$

10. Answer (C)

Hint : Put the value of $T_{0}$.

## Solution :

$\because T=T_{0}-0.006 h_{0}$
$\Rightarrow 273=224-0.006 \times h_{0}$
$\Rightarrow h_{0}=8170 \mathrm{~m}$
11. Answer (C)

Hint : Put the value of $h_{0}$.

## Solution :

$$
\begin{aligned}
P & =P_{0}\left(1-\frac{0.006 \times 8170}{273}\right) \frac{29 \times 10^{-3} \times 9.8}{8.31 \times 0.006} \\
& =P_{0} \times(0.82)^{5.7} \\
& =0.32 P_{0}
\end{aligned}
$$

12. Answer (A)

Hint: $P^{1-\gamma} T^{\gamma}=$ constant

## Solution :

$P_{1}^{1-\gamma} T_{1}^{\gamma}=P_{2}^{1-\gamma} T_{2}^{\gamma}$
$\Rightarrow T_{2}=1000 \times\left(\frac{3}{2}\right)^{\left(\frac{3}{5}-1\right)}=850 \mathrm{~K}$
Then, $\frac{P_{3}}{T_{3}}=\frac{P_{2}}{T_{2}} \Rightarrow T_{3}=425 \mathrm{~K}$
$\therefore \quad \Delta Q=n C_{v} \Delta T=1 \times\left(\frac{3 R}{2}\right) \times(850-425)$

$$
=5300 \mathrm{~J}
$$

13. Answer (B)

Hint : Use concept of standing wave.
Solution :

$$
\begin{aligned}
y=y_{1} & +y_{2} \\
& =a\left[\sin \left(\frac{\pi}{2} x-\omega t\right)+\sin \left(\frac{\pi}{2} x+\omega t+\frac{\pi}{3}\right)\right] \\
\Rightarrow y & =2 a \sin \left(\frac{\pi}{2} x+\frac{\pi}{6}\right) \cdot \cos \left(\cot +\frac{\pi}{6}\right)
\end{aligned}
$$

For nodes, $2 a \sin \left(\frac{\pi}{2} x+\frac{\pi}{6}\right)=0$
$\Rightarrow \quad \frac{\pi}{2} x+\frac{\pi}{6}=\pi, 2 \pi, 3 \pi, 4 \pi, \ldots$.
$\Rightarrow \quad x=\frac{5}{3}, \frac{11}{3}, \frac{17}{3}, \frac{23}{3}$
$\therefore$ For $0 \leq x \leq 6$,
Number of nodes $=3$
14. Answer (C)

Hint: Flux $=\frac{q}{4 \pi \varepsilon_{0}} \times$ Solid angle $\times 2$

## Solution :

$$
\begin{aligned}
\phi & =\frac{q}{\varepsilon_{0}} \times \frac{2 \pi(1-\cos \theta)}{4 \pi} \times 2 \\
& =\frac{q}{\varepsilon_{0}}\left(1-\frac{\ell}{\sqrt{\ell^{2}+R^{2}}}\right)=\frac{q}{\varepsilon_{0}}\left(1-\frac{2}{\sqrt{5}}\right)
\end{aligned}
$$

15. Answer (B)

Hint : Use KVL and KCL

## Solution :

For $R_{A B}$


$$
\therefore \quad R_{A B}=\frac{7 R}{12}
$$

For $R_{A C}$

$\therefore \quad R_{A C}=\frac{3 R}{4}$
$\therefore \quad \frac{R_{A B}}{R_{A C}}=\frac{7 \times 4}{12 \times 3}=\frac{7}{9}$
16. Answer $A(R, T) ; B(S, T) ; C(Q, S) ; D(Q, S)$

Hint : In isothermal process $\Delta U=0$
Solution :
For A : PV = constant
$\Rightarrow \Delta U=0, \Delta W=$ positive
$\Rightarrow \Delta Q=$ positive
For $\mathrm{B}: ~ P=\frac{p R T}{m} \Rightarrow T=$ constant
$\Rightarrow \Delta U=0, \Delta W=-$ negative, $\Delta Q=$ negative
And so on.
17. Answer $A(P, R) ; B(P, S) ; C(Q, T) ; D(Q, S)$

Hint : After earthing, charge on outer surface of outer most plates becomes zero.
Solution :
Before earthing


After earthing


$$
V_{A B}=\frac{Q d}{\varepsilon_{0} A}, V_{B C}=\frac{3 Q d}{\varepsilon_{0} A}, V_{C D}=0, V_{D E}=\frac{3 Q d}{\varepsilon_{0} A}
$$

18. Answer (06)

Hint : Use superposition principle.
Solution :
$E_{1}=\frac{Q}{4 \pi \varepsilon_{0} a^{2}}$

$\therefore \quad E_{\text {net }}=3 \times\left(E_{1} \cos \theta\right)=3 \times \frac{Q}{4 \pi \varepsilon_{0} a^{2}} \times \sqrt{\frac{2}{3}}$

$$
=\frac{Q \sqrt{6}}{4 \pi \varepsilon_{0} a^{2}}
$$

19. Answer (01)

Hint : Use Newton's law.

## Solution :

$\frac{-d T}{d t}=b\left(T-T_{s}\right)$
$\Rightarrow \quad \Delta T=(\Delta T)_{0} e^{-b t}$
$\therefore t_{2}=2 t_{0}$
$\therefore \quad n=1$
20. Answer (02)

Hint : Reduce it to a finite circuit.

## Solution :

$R_{A B}=R_{C D}, V_{C D}=\frac{1}{2} V_{A B}$
$\therefore \quad$ Current gets equally distributed
$\therefore \quad R_{2}=R_{A B}$
And, $R_{A B}=R_{1}+\left(\frac{R_{2}}{2}\right)=R_{2}$
$\Rightarrow \frac{R_{2}}{R_{1}}=2$

## PART - II (CHEMISTRY)

21. Answer (C, D)

Hint :

P is


Solution :
$Q$ is

22. Answer (A, C, D)
 is more basic than aniline

## Solution :



are less basic than aniline
23. Answer (D)


Solution :


Racemic mixture
24. Answer (A, C, D)

Hint :



## Solution :

$Q$ is slightly basic
P contains fluorine atom
Because of the presence of $-\mathrm{NH}_{2}$ group, Q can give coupling reaction
25. Answer (B, C, D)

Hint : Benzaldehyde is not oxidised by Fehling's reagent.

## Solution :

Acetophenone can give iodoform and bromoform.
26. Answer (D)

Hint : Given D-glyceraldehyde is ' $R$ '


## Solution :


$R$ as well as $D$.
27. Answer (B)

Hint : D and L convention is used for amino acids also
Solution :
(D) fructose is laevorotatory (I)
(D) glucose is dextrorotatory (d)
28. Answer (A)

Hint : Product obtained after ozonolysis


Solution :
$C^{*}$ is $L$
$C^{\#}$ is $D$.
29. Answer (B)
30. Answer (A)
31. Answer (B)

Hint and Solution : Q. Nos. 29 to 31

(B)


## Solution :





32. Answer (A)

Hint : Excess of ether and water as solvent will favour $S_{N} 1$ reaction.

## Solution :


33. Answer (C)

Hint :


Solution :

34. Answer (B)

Hint :

(P)
(Q)

Solution :



Possible Products
40. Answer (07)

Hint :


## Solution :

$x=1, y=2, z=4$

## PART - III (MATHEMATICS)

41. Answer (B, C)

Hint: Perpendicularity of two lines.

## Solution :

$L_{1}$ and $L_{2}$ if they are $\perp$ to a common line $\Rightarrow \lambda=-1$ for two adjacent sides of a square
$L_{1} \perp L_{2}$
$\therefore\left(\lambda^{2}+1\right) \lambda^{2}=1$
$\Rightarrow \lambda^{5}+2 \lambda^{3}+\lambda-1=0=f(\lambda)$
$\therefore f^{\prime}(\lambda)=5 \lambda^{4}+6 \lambda^{2}+1=0$
$\therefore f(\lambda)=0$ has only one real root
42. Answer (A, B)

Hint : Condition of two degree equation (to represent pair of straight line.

## Solution :

$\Delta=0 \Rightarrow a b c+2 f g h=a f^{2}+b g^{2}+c h^{2}$
$\Rightarrow c=\frac{-10}{9}$
Also
$\cos \alpha=\left|\frac{a+b}{\sqrt{(a-b)^{2}+4 h^{2}}}\right| \Rightarrow \alpha=\cos ^{-1}\left(\frac{5}{\sqrt{34}}\right)$
43. Answer (A)

Hint : Division formula between two points.

Solution :

$$
A\left(\frac{a b}{a+b}\left(\frac{1-m}{-m}, 0\right): B\left(-0, \frac{a b}{a+b}(1-m)\right)\right.
$$

Mid-point of $A B$ is $(h, k)$
$\therefore 2 h=\frac{a b}{a+b} \frac{(m-1)}{m} ; 2 k \frac{a b}{a+b}(1-m)$
$\therefore \frac{1}{2 h}+\frac{1}{2 k}=\frac{a+b}{a b}$
$\Rightarrow \mathrm{ab}(x+y)=2(a+b) x y$ is the locus
Let $P$ divides $A B$ in ratio 1:3
$\therefore P\left(\frac{\frac{3 a b}{a+b}\left(1-\frac{1}{m}\right)}{4}, \frac{a b}{a+b}(1-m)\right)$
$\therefore(x+3 y) a b \equiv 4(a+b) x y$ is the required locus
44. Answer (B, D)

Hint : Distance between two parallel lines.

## Solution :

Distance between two parallel lines $=2 \sqrt{5}$
$\therefore$ points on line $\frac{x-1}{-2}=\frac{y+2}{1}= \pm 2 \sqrt{5}$

$$
\overline{\sqrt{5}} \quad \frac{\dot{\sqrt{5}}}{}
$$

$\therefore$ points are $(-3,0)$ and $(5,-4)$
$\therefore$ Required lines are

$$
2 x-y+6=0 \text { and } 2 x-y-14=0
$$

45. Answer (B, C)

Hint : Translation and Rotation of axes.

## Solution :

For $f(x, y)=0$
new origin=
$\left(\frac{h f-b h}{a b-h^{2}}, \frac{g f-a f}{a b-h^{2}}\right) \equiv\left(\frac{28}{-14}, \frac{42}{-14}\right) \equiv(-2,-3)$
For $g(x, y)=0$
$\theta=\frac{1}{2} \tan ^{-1}\left(\frac{2 h}{a-b}\right)=\frac{1}{2} \tan ^{-1}\left(\frac{2 \times \sqrt{3}}{2}\right)$
$=\frac{1}{2} \times \frac{\pi}{3}=\frac{\pi}{6}$
46. Answer (C)

Hint : Family of circle with line.

## Solution :

Let required circle
$x^{2}+y^{2}-3 x+2 y-4+\lambda(2 x+5 y+2)=0$
$\therefore C\left(\frac{3-2 \lambda}{2}, \frac{-(5 \lambda+2)}{2}\right)$ satisfy $x+y=11$
$\therefore \lambda=-3$
$\therefore$ Required circle is $x^{2}+y^{2}-9 x-13 y-10=0$
47. Answer (D)

Hint: Orthogonal of two circles.

## Solution :

Let required circle
$(x-1)^{2}+(y+1)^{2}+\lambda(2 x+3 y+1)=0$
Circle with diameter points $(0,3)$ and $(-2,-1)$ is
$x^{2}+y^{2}+2 x-2 y-3=0$
(i) of (ii) intersect orthogonally
$\therefore(2 \lambda-1)+-2\left(\frac{3 \lambda}{2}+1\right)=\lambda-1 \Rightarrow \lambda=\frac{-3}{2}$
Required circle is $2 x^{2}+2 y^{2}-10 x-5 y+1=0$
48. Answer (A)

Hint : Touching concept of line with circle.

## Solution :

Let required circle
$\left(x^{2}+y^{2}-4\right)+\lambda(x+2 y-4)=0$
$C\left(\frac{-\lambda}{2},-\lambda\right)=\lambda=\sqrt{\frac{5 \lambda^{2}}{4}+4 \lambda+4}$
$\because$ it touches line $x+2 y-5=0$
$\therefore\left|\frac{\frac{-\lambda}{2}+2(-\lambda)-5}{\sqrt{5}}\right|=\sqrt{\frac{5 \lambda^{2}}{4}+4 \lambda+4}$
$\Rightarrow 5(\lambda+2)^{2}=5 \lambda^{2}+16 \lambda+16$
$\Rightarrow \lambda=-1$
$\therefore$ Required circle $x^{2}+y^{2}-x-2 y=0$
49. Answer (D)

Hint : Chord of contact of circle.

## Solution :

Equation of C.O.C $h x+k y=8$
Also $t k=h+2 t^{2}$ (ii) $\because(h, k)$ satisfy tangent)
$\Rightarrow h x+y \frac{\left(h+2 t^{2}\right)}{t}-8=0$
$\Rightarrow 2(t y-4)+h\left(x+\frac{y}{t}\right)=0$
$\therefore \quad$ Line passes through point
$y=\frac{4}{t}$ and $x=\frac{-y}{t}$
$\Rightarrow \frac{y}{4}=-\frac{x}{y} \Rightarrow y^{2}=-4 x$
50. Answer (A)

Hint : Point of intersection of two curves.

## Solution :

Point of intersection of $x=-2$ and $x^{2}+y^{2}=16$
$\therefore y^{2}=12 \Rightarrow y= \pm 2 \sqrt{3}$
$\therefore$ Point $(-2,2 \sqrt{3})$
51. Answer (C)

Hint : Circumcircle of triangle $A B C$

## Solution :

The equation of the circumcircle of $\triangle A Q B$ is
$\left(x^{2}+y^{2}-8\right)+\lambda(h x+k y-8)=0 \because(\mathrm{~A}=-1)$ due to $(0,0)$ satisfy it
$\therefore$ Equation is $x^{2}+y^{2}-h x-k y=0$
Now centre $\left(\frac{h}{2}, \frac{k}{2}\right)$
$\therefore$ For locus let $x=\frac{h}{2} ; y=\frac{k}{2}$
$h=2 x$ and $k=2 y$
$\because t k=h+2 t^{2} \therefore$ at $t=2$
The required locus is $2 y=x+4$
52. Answer (C)

Hint : I.T.F. conversion in domain.

Solution :
Let $\sin ^{-1} x=\theta \Rightarrow x=\sin \theta$
Now
$\cos ^{-1} x=\cos ^{-1}(\sin \theta)=\cos ^{-1}\left(-\cos \left(\frac{3 \pi}{2}-\theta\right)\right)$
$=\pi-\cos ^{-1}\left(\cos \left(\frac{3 \pi}{2}-\theta\right)\right)$
$=\pi-\left(\frac{3 \pi}{2}-\theta\right)$ as $\frac{3 \pi}{2}-\theta \in(0, \pi)$
$=\theta-\frac{\pi}{2}=\sin ^{-1} x-\frac{\pi}{2}$
$\therefore \sin ^{-1} x+\cos ^{-1} x=2 \sin ^{-1} x-\frac{\pi}{2}$
53. Answer (A)

Hint : Locus of midpoint of Parallel chords.

## Solution :

Let middle point is $(h, k)$
$\therefore \quad$ Equation of chord in mid-point form is
$\frac{x}{h}+\frac{y}{k}=2$
$\therefore-\frac{1}{h \times \frac{1}{k}}=m \Rightarrow k=-m h$
$\Rightarrow y+m x=0$ is the required locus
54. Answer (B)

Hint : Condition of common tangent on two curves.

## Solution :

$y=\frac{x}{2}+2$ is tangent on $\frac{x^{2}}{4}+\frac{y^{2}}{b^{2}}=1$
$\Rightarrow 4+4 b^{2}=16 \Rightarrow b^{2}+1=4 \Rightarrow b= \pm \sqrt{3}$
Now tangent at other point is given by $-2 y=x+4$
$\Rightarrow x+2 y+4=0$
55. Answer (D)

Hint : Length of latus rectum independency.

## Solution :


$\theta=2 \tan ^{-1} 2$
$\because \sqrt{3}<2<\sqrt{2}+1$
$\frac{\pi}{3}<\tan ^{-1} 2<\frac{3 \pi}{8}$
$\Rightarrow \frac{2 \pi}{3}<\theta<\frac{3 \pi}{-4}$
56. Answer A(P, Q); B(P, Q); C(R, T); D(S, T)

Hint : Property of perpendicular normals.

## Solution :

Equation of normal at ' $p$ ' is
$y=-t x+2 a t+a t^{3}$
Put $y=-2 a t \Rightarrow x=4 a+a t^{2}$
$\therefore G\left(4 a+a t^{2},-2 a t\right)$
Required locus $y^{2}=4 a(x-4 a)$

$$
\because a=1
$$

$\therefore y^{2}=4(x-4)$
Now verify each option
57. Answer $A(P) ; B(Q) ; C(Q, S) ; D(R, S)$

Hint : Type of functions concept.

## Solution :

(A) $f(x)= \begin{cases}\left((1)^{1}\right)^{n} x>0=1 & , x>0 \\ \left((-1)^{-1}\right)^{n} x<0 & , x<0\end{cases}$
$f(x)$ is an odd function. $f(x)$ is not bijective
$\because f(x)$ is not one one
(B) $f(x)=\frac{x}{e^{x}-1}+\frac{x}{2}+1$
$f(x)=\frac{-x}{e^{-x}-1}-\frac{x}{2}+1=x+\frac{x}{e^{x}-1}-\frac{x}{2}+f(x)$
$\therefore f(x)$ is an even function $\because f(x)$ is not bijective
(C) $f(-x)=f(x) \therefore f(x)$ is even. $f(x)$ is periodic but time period not define
(D) $f(x)=\max \{\tan x, \cot x\}$. From graph of $f(x)$ it is clear that
$f(x)$ is neither even nor odd
$\because f(x+\pi)=\max \{\tan (x+\pi), \cot (x+\pi)\}$
$=\max \{\tan x, \cot x\} f(x)$ is periodic with $\mathrm{f}(\mathrm{x})$ is periodic with $\pi$
58. Answer (03)

Hint : Graphical solution.

## Solution :



From graph it is clear that curves intersect at 3 points
$\therefore$ Only 3 solutions
59. Answer (00)

Hint : Trigonometric conversion of I.T.F.

## Solution :

$$
\begin{aligned}
& \sin \left(\cos ^{-1}\left(\tan \left(\tan ^{-1}\left(\sqrt{x^{2}-1}\right)\right)\right)\right) \\
& =\sin \left(\cos ^{-1} \sqrt{x^{2}-1}\right)
\end{aligned}
$$

$$
\begin{aligned}
& =\sin \left(\sin ^{-1} \sqrt{2-x^{2}}\right)=\sqrt{2-x^{2}} \\
& \therefore \text { Common domain }[1, \sqrt{2}] \Rightarrow 2-x^{2}=1+x \\
& \Rightarrow x^{2}+x-1=0 \Rightarrow x=\frac{-1 \pm \sqrt{5}}{2} \\
& x=\frac{\sqrt{5}-1}{2} \notin[1, \sqrt{2}]
\end{aligned}
$$

$\therefore$ No solution exists
60. Answer (09)

Hint : Sum of infinite G.P.

## Solution :

$$
\begin{aligned}
& \frac{1}{1-\sin \left(\cos ^{-1} x\right)}=2 \\
& \Rightarrow \sin \left(\cos ^{-1} x\right)=\frac{1}{2} \\
& \Rightarrow \cos ^{-1} x=\frac{\pi}{6} \Rightarrow x=\frac{\sqrt{3}}{2} \Rightarrow 4 x^{2}=3 \\
& \Rightarrow 12 x^{2}=9
\end{aligned}
$$

