# All India Aakash Test Series for JEE (Advanced)-2020

# TEST - 2A (Paper-2) - Code-E

Test Date : 24/11/2019

# **ANSWERS**

| PHYSICS |                        | CHE | CHEMISTRY     |     | MATHEMATICS   |  |
|---------|------------------------|-----|---------------|-----|---------------|--|
| 1.      | (B, D)                 | 21. | (B, C, D)     | 41. | (B, C)        |  |
| 2.      | (B, D)                 | 22. | (A, C, D)     | 42. | (B, D)        |  |
| 3.      | (A, D)                 | 23. | (D)           | 43. | (A)           |  |
| 4.      | (B, C)                 | 24. | (A, C, D)     | 44. | (A, B)        |  |
| 5.      | (A)                    | 25. | (C, D)        | 45. | (B, C)        |  |
| 6.      | (D)                    | 26. | (D)           | 46. | (C)           |  |
| 7.      | (B)                    | 27. | (B)           | 47. | (D)           |  |
| 8.      | (C)                    | 28. | (A)           | 48. | (A)           |  |
| 9.      | (A)                    | 29. | (B)           | 49. | (D)           |  |
| 10.     | (C)                    | 30. | (A)           | 50. | (A)           |  |
| 11.     | (C)                    | 31. | (B)           | 51. | (C)           |  |
| 12.     | (B)                    | 32. | (A)           | 52. | (D)           |  |
| 13.     | (C)                    | 33. | (B)           | 53. | (B)           |  |
| 14.     | (B)                    | 34. | (C)           | 54. | (A)           |  |
| 15.     | (A)                    | 35. | (A)           | 55. | (C)           |  |
| 16.     | $A \rightarrow (P, R)$ | 36. | $A \to (Q,S)$ | 56. | $A \to (P)$   |  |
|         | $B \to (P,S)$          |     | $B \to (R)$   |     | $B \to (Q)$   |  |
|         | $C \to (Q,T)$          |     | $C \to (Q,R)$ |     | $C \to (Q,S)$ |  |
|         | $D \to (Q,S)$          |     | $D \to (P,T)$ |     | $D \to (R,S)$ |  |
| 17.     | $A \rightarrow (R, T)$ | 37. | $A \to (Q,S)$ | 57. | $A \to (P,Q)$ |  |
|         | $B \to (S,T)$          |     | $B \to (Q)$   |     | $B \to (P,Q)$ |  |
|         | $C \to (Q,S)$          |     | $C \to (R,T)$ |     | $C \to (R,T)$ |  |
|         | $D \to (Q,S)$          |     | $D\to(Q)$     |     | $D\to(S,T)$   |  |
| 18.     | (02)                   | 38. | (07)          | 58. | (09)          |  |
| 19.     | (01)                   | 39. | (03)          | 59. | (00)          |  |
| 20.     | (06)                   | 40. | (06)          | 60. | (03)          |  |

# **HINTS & SOLUTIONS**

# PART - I (PHYSICS)

1. Answer (B, D)

Hint : *B* and *C* will be in series. Solution :

 $C_{BC} = \frac{2 \times 3}{2 + 3} = \frac{6}{5} \mu F$  $\therefore \quad \Delta q_{S} = \frac{\frac{6}{5}}{\frac{6}{5} + 1} \times 110 = 60 \ \mu C$ 

$$\therefore \quad q_A = 110 - 60 = 50 \ \mu\text{C}$$
$$V_B = \frac{60}{2} = 30 \ \text{V}, \ V_C = \frac{60}{3} = 20 \ \text{V}$$

2. Answer (B, D)

Hint : Particle performs SHM. Solution :

$$E = \frac{Qx}{4\pi\varepsilon_0 (R^2 + x^2)^{\frac{3}{2}}}, \quad x \ll R$$
  

$$\Rightarrow \quad E = \frac{Qx}{4\pi\varepsilon_0 R^3}$$
  

$$\therefore \quad \omega = \sqrt{\frac{Qq}{m \times 4\pi\varepsilon_0 R^3}}$$
  

$$\therefore \quad T = 2\pi \sqrt{\frac{m \times 4\pi\varepsilon_0 R^3}{Qq}} = 4\pi \sqrt{\frac{\pi\varepsilon_0 m R^3}{Qq}}$$
  
and,  $V_{max} = \omega a = \frac{ax}{2} \sqrt{\frac{Qq}{\pi\varepsilon_0 m R^3}}$ 

3. Answer (A, D)

Hint : Frequency as well as wavelength change. Solution :

. .

$$\lambda_{1} = \lambda_{0} - \frac{V}{5}T \implies \lambda_{1} = \frac{4\lambda_{0}}{5}$$
$$\therefore \quad \lambda_{2} = 2\lambda_{1} = \frac{8\lambda_{0}}{5}$$
and, 
$$T' = \frac{\lambda'}{2V + \frac{V}{5}} = \frac{5\lambda'}{11V}$$
$$\therefore \quad f' = \frac{1}{T'} = \frac{11V}{5 \times \left(\frac{8\lambda_{0}}{5}\right)} = \frac{11V}{8f_{0}}$$

4. Answer (B, C) Hint :  $\Delta Q = \Delta U + \Delta W$ Solution :  $Q = \Delta U + \frac{Q}{2} \implies \Delta U = \frac{Q}{2}$   $\Rightarrow n \times \left(\frac{3R}{2}\right) \cdot \Delta T = \frac{nC\Delta T}{2}$   $\Rightarrow C = 3R$ And,  $\Delta U = \Delta W$   $\Rightarrow n\left(\frac{3R}{2}\right) \cdot dT = PdV$   $\Rightarrow P^3 V = \text{constant}$   $\Rightarrow P^2 \times T = \text{constant}$  $\Rightarrow P \propto \frac{1}{\sqrt{T}}$ 

5. Answer (A)

Hint : A balanced wheatstone bridge is formed.

# Solution :

$$\therefore V_D - V_C = 0$$
  
$$\therefore R_{eq} = \frac{12 \times 6}{12 + 6} = 4 \Omega$$
  
$$\therefore I_{battery} = \frac{20}{4} = 5 A$$
  
$$I_{AD} = \frac{20}{12} = \frac{5}{3} A$$

**Hint :** Two spheres behave as capacitor and then become in parallel finally.

# Solution :

$$Q_{0} = 4\pi\varepsilon_{0} (2a) \times V$$
  

$$\therefore \quad i = \frac{V}{R} e^{-\frac{t}{\tau}}, \quad \tau = R \times \left(\frac{C_{1}C_{2}}{C_{1} + C_{2}}\right)$$
  

$$= R \times \frac{4\pi\varepsilon_{0}a \times 2a}{3a}$$
  

$$= \frac{8\pi\varepsilon_{0}Ra}{3}$$
  

$$\therefore \quad i = \frac{V}{R} e^{-\frac{3t}{8\pi\varepsilon_{0}Ra}}$$

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

#### 7. Answer (B)

**Hint :** Two spheres behave as capacitor and then become in parallel finally.

#### Solution :

Final charge on smaller sphere

$$q_{2} = \frac{C_{2}}{C_{1} + C_{2}} \times Q_{0}$$
$$= \frac{4\pi\varepsilon_{0} \times a}{4\pi\varepsilon_{0} (a + 2a)} \times \left[4\pi\varepsilon_{0} \times (2a) \times V\right]$$
$$= \frac{1}{3} \times 8\pi\varepsilon_{0} aV$$

8. Answer (C)

**Hint :** Two spheres behave as capacitor and then become in parallel finally.

#### Solution :

Total heat dissipation

$$H = \frac{1}{2} \times \left(\frac{C_1 C_2}{C_1 + C_2}\right) \times V^2$$
$$= \frac{1}{2} \times \frac{2}{3} \times (4\pi \varepsilon_0 a) V^2$$
$$= \frac{4\pi \varepsilon_0 a V^2}{3}$$

9. Answer (A)

**Hint** : Speed of sound,  $V = \sqrt{\frac{\gamma RT}{M}}$ 

Solution :

$$V = \sqrt{\frac{\gamma RT}{M}}$$
  

$$\Rightarrow T = \frac{V^2 M}{\gamma R} = \frac{(300)^2 \times (29 \times 10^{-3})}{1.4 \times 8.314}$$
  

$$\approx 224 \text{ K}$$

10. Answer (C)

**Hint :** Put the value of  $T_0$ .

Solution :

- ::  $T = T_0 0.006 h_0$
- $\Rightarrow$  273 = 224 0.006 ×  $h_0$

$$\Rightarrow h_0 = 8170 \text{ m}$$

11. Answer (C)

**Hint :** Put the value of  $h_0$ .

Solution :

$$P = P_0 \left( 1 - \frac{0.006 \times 8170}{273} \right) \frac{29 \times 10^{-3} \times 9.8}{8.31 \times 0.006}$$
$$= P_0 \times (0.82)^{5.7}$$
$$= 0.32 P_0$$

12. Answer (B)

Hint : Use KVL and KCL

# Solution :

For R<sub>AB</sub>



$$\therefore R_{AB} = \frac{7R}{12}$$

For R<sub>AC</sub>



$$\therefore \quad R_{AC} = \frac{3R}{4}$$

$$\therefore \quad \frac{R_{AB}}{R_{AC}} = \frac{7 \times 4}{12 \times 3} = \frac{7}{9}$$

13. Answer (C)

**Hint :** Flux 
$$= \frac{q}{4\pi\varepsilon_0} \times \text{Solid angle} \times 2$$

#### Solution :

$$\phi = \frac{q}{\varepsilon_0} \times \frac{2\pi(1 - \cos\theta)}{4\pi} \times 2$$
$$= \frac{q}{\varepsilon_0} \left( 1 - \frac{\ell}{\sqrt{\ell^2 + R^2}} \right)$$
$$= \frac{q}{\varepsilon_0} \left( 1 - \frac{2}{\sqrt{5}} \right)$$

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020 Test - 2A (Paper-2) (Code-E)\_(Hints & Solutions)

#### 14. Answer (B)

Hint : Use concept of standing wave.

### Solution :

$$y = y_1 + y_2$$
  
=  $a \left[ sin\left(\frac{\pi}{2}x - \omega t\right) + sin\left(\frac{\pi}{2}x + \omega t + \frac{\pi}{3}\right) \right]$   
 $\Rightarrow \quad y = 2a sin\left(\frac{\pi}{2}x + \frac{\pi}{6}\right) \cdot cos\left(cot + \frac{\pi}{6}\right)$ 

For nodes,  $2a\sin\left(\frac{\pi}{2}x+\frac{\pi}{6}\right)=0$ 

$$\Rightarrow \frac{\pi}{2}x + \frac{\pi}{6} = \pi, 2\pi, 3\pi, 4\pi, \dots$$
5 11 17 23

$$\Rightarrow x = \frac{5}{3}, \frac{11}{3}, \frac{17}{3}, \frac{23}{3}$$

$$\therefore \quad \text{For } 0 \le x \le 6,$$

Number of nodes = 3

15. Answer (A)

**Hint :**  $P^{1-\gamma}$   $T^{\gamma}$  = constant

#### Solution :

$$P_1^{1-\gamma}T_1^{\gamma} = P_2^{1-\gamma}T_2^{\gamma}$$

$$\Rightarrow T_2 = 1000 \times \left(\frac{3}{2}\right)^{\left(\frac{3}{5}-1\right)} = 850 \text{ K}$$
Then,  $\frac{P_3}{T_3} = \frac{P_2}{T_2} \Rightarrow T_3 = 425 \text{ K}$ 

$$\therefore \quad \Delta Q = nC_v \Delta T = 1 \times \left(\frac{3R}{2}\right) \times (850 - 425)$$

16. Answer A(P, R); B(P, S); C(Q, T); D(Q, S)

**Hint :** After earthing, charge on outer surface of outer most plates becomes zero.

#### Solution :

Before earthing





17. Answer A(R, T); B(S, T); C(Q, S); D(Q, S) **Hint :** In isothermal process  $\Delta U = 0$  **Solution :** For A : *PV* = constant  $\Rightarrow \Delta U = 0, \Delta W = \text{positive}$  $\Rightarrow \Delta Q = \text{positive}$ 

For B : 
$$P = \frac{pRT}{m} \Rightarrow T = \text{constant}$$
  
 $\Rightarrow \Delta U = 0, \Delta W = -\text{negative}, \Delta Q = \text{negative}$   
And so on.

18. Answer (02)

Hint : Reduce it to a finite circuit.

Solution :

$$R_{AB} = R_{CD}, \ V_{CD} = \frac{1}{2} V_{AB}$$

- ... Current gets equally distributed
- $\therefore$   $R_2 = R_{AB}$

And, 
$$R_{AB} = R_1 + \left(\frac{R_2}{2}\right) = R_2$$

$$\Rightarrow \frac{R_2}{R_1} = 2$$

19. Answer (01)

Hint : Use Newton's law.

Solution :

$$\frac{-dT}{dt} = b(T - T_s)$$

$$\Rightarrow \Delta T = (\Delta T)_0 e^{-bt}$$

$$\therefore t_2 = 2t_0$$

$$\therefore n = 1$$

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# 20. Answer (06)

Hint : Use superposition principle. Solution :



# PART - II (CHEMISTRY)

Answer (B, C, D)
 Hint : Benzaldehyde is not oxidised by Fehling's reagent.

# Solution :

Acetophenone can give iodoform and bromoform.

22. Answer (A, C, D) Hint :



# Solution :

Q is slightly basic

P contains fluorine atom

Because of the presence of  $-NH_2$  group, Q can give coupling reaction

23. Answer (D)

Hint : Leucine is 
$$HC - H_2C - C - COOH$$
  
 $CH_3$   $HH_2$   
Solution :  
 $CO_2C_2H_5$   $CO_2C_2H_5$   
 $CH - CO_2C_2H_5$   $HC - CO_2C_2H_5$   
 $CH - CO_2C_2H_5$   $HL_2$   
 $CH_3$   $CO_2C_2H_5$   
 $CH_3$   $H_2$   
 $CH_3$   $H_2$   
 $CH_3$   $CO_2C_2H_5$   
 $CH_3$   $CO_2C_2H_5$   
 $H_3$   $CO_2C_2H_5$   
 $CH_3$   $H_2$   
 $CH_3$   $CO_2C_2H_5$   
 $CO_2C_2H_5$   
 $CO_$ 

24. Answer (A, C, D) NH (CH<sub>4</sub>)

Hint : O is more basic than aniline

10



are less basic than aniline

25. Answer (C, D)

Solution :

Hint :



Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020 Test - 2A (Paper-2) (Code-E)\_(Hints & Solutions)





26. Answer (D)

Hint : Given D-glyceraldehyde is 'R'



Solution :



R as well as D.

27. Answer (B)

**Hint :** D and L convention is used for amino acids also

#### Solution :

- (D) fructose is laevorotatory (I)
- (D) glucose is dextrorotatory(d)

28. Answer (A)

Hint : Product obtained after ozonolysis





Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# 32. Answer (A)

Hint : It is electrophilic substitution reaction.

# Solution :

The intermediate formed when  ${}^{+}NO_{2}$  attacks at position C-2 is more stable.

#### 33. Answer (B)

# Hint :



Solution :



34. Answer (C)

Hint :



Solution :



35. Answer (A)

Hint : Excess of ether and water as solvent will favour  $S_N 1$  reaction.

# Solution :



36. Answer A(Q, S); B(R); C(Q, R); D(P, T)

Hint :



Solution :



Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020

Test - 2A (Paper-2) (Code-E)\_(Hints & Solutions)



37. Answer A(Q, S); B(Q); C(R, T); D(Q)

**Hint :** LiAIH<sub>4</sub> is a very strong reducing agent can reduce almost functional groups to lower oxidation state, except alkenes and alkynes.

# Solution :

NaBH<sub>4</sub> cannot reduce amide into amine

NaBH<sub>4</sub> can reduce only acid halide into alcohol among the given transformation.

38. Answer (07)



Solution :

x = 1, y = 2, z = 4

39. Answer (03)

Hint :



#### Solution :



Possible Products

40. Answer (06)

**Hint :** O, P-substituted Bromo group are more likely to get substituted.

# Solution :

The Br group at position 4 is most likely to get substitute and at position 2, is least

# **PART - III (MATHEMATICS)**

41. Answer (B, C)

Hint : Translation and Rotation of axes.

Solution :

For f(x,y) = 0

new origin=

$$\left(\frac{hf-bh}{ab-h^2},\frac{gf-af}{ab-h^2}\right) \equiv \left(\frac{28}{-14},\frac{42}{-14}\right) \equiv \left(-2,-3\right)$$

For g(x,y) = 0

$$\theta = \frac{1}{2} \tan^{-1} \left( \frac{2h}{a-b} \right) = \frac{1}{2} \tan^{-1} \left( \frac{2 \times \sqrt{3}}{2} \right)$$

$$=\frac{1}{2}\times\frac{\pi}{3}=\frac{\pi}{6}$$

42. Answer (B, D)

Hint : Distance between two parallel lines.

Solution :

Distance between two parallel lines =  $2\sqrt{5}$ 

- $\therefore \text{ points on line } \frac{x-1}{\frac{-2}{\sqrt{5}}} = \frac{y+2}{\frac{1}{\sqrt{5}}} = \pm 2\sqrt{5}$
- $\therefore$  points are (-3, 0) and (5, -4)
- :. Required lines are

$$2x - y + 6 = 0$$
 and  $2x - y - 14 = 0$ 

43. Answer (A)

Hint : Division formula between two points.

Solution :

$$A\left(\frac{ab}{a+b}\left(\frac{1-m}{-m},0\right):B\left(-0,\frac{ab}{a+b}\left(1-m\right)\right)$$

Mid-point of AB is (h, k)

$$\therefore 2h = \frac{ab}{a+b} \frac{(m-1)}{m}; 2k \frac{ab}{a+b} (1-m)$$

$$\therefore \frac{1}{2h} + \frac{1}{2k} = \frac{a+b}{ab}$$

 $\Rightarrow$  ab (x + y) = 2 (a + b) xy is the locus

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

$$\therefore P\left(\frac{\frac{3ab}{a+b}\left(1-\frac{1}{m}\right)}{4}, \frac{\frac{ab}{a+b}\left(1-m\right)}{4}\right)$$

 $\therefore$  (*x* + 3*y*)*ab* = 4(*a* + *b*)*xy* is the required locus

#### 44. Answer (A, B)

**Hint :** Condition of two degree equation (to represent pair of straight line.

#### Solution :

$$\Delta = 0 \Rightarrow abc + 2fgh = af^2 + bg^2 + ch^2$$

 $\Rightarrow c = \frac{-10}{9}$ 

Also

$$\cos \alpha = \left| \frac{a+b}{\sqrt{(a-b)^2 + 4h^2}} \right| \Rightarrow \alpha = \cos^{-1} \left( \frac{5}{\sqrt{34}} \right)$$

45. Answer (B, C)

Hint : Perpendicularity of two lines.

#### Solution :

 $L_1$  and  $L_2$  if they are  $\perp$  to a common line  $\Rightarrow \lambda = -1$  for two adjacent sides of a square

$$L_1 \perp L_2$$

$$\therefore (\lambda^2 + 1) \lambda^2 = 1$$

$$\Rightarrow \lambda^5 + 2\lambda^3 + \lambda - 1 = 0 = f(\lambda)$$

- $\therefore f'(\lambda) = 5\lambda^4 + 6\lambda^2 + 1 = 0$
- $\therefore$   $f(\lambda) = 0$  has only one real root
- 46. Answer (C)

Hint : Family of circle with line.

#### Solution :

Let required circle

$$x^2 + y^2 - 3x + 2y - 4 + \lambda (2x + 5y + 2) = 0$$

$$\therefore C\left(\frac{3-2\lambda}{2}, \frac{-(5\lambda+2)}{2}\right) \text{ satisfy } x+y=11$$

 $\therefore \lambda = -3$ 

 $\therefore$  Required circle is  $x^2 + y^2 - 9x - 13y - 10 = 0$ 

47. Answer (D)

Hint : Orthogonal of two circles.

## Solution :

Let required circle

$$(x-1)^2 + (y+1)^2 + \lambda(2x+3y+1) = 0$$
 (i)

Circle with diameter points (0,3) and (-2,-1) is

$$x^2 + y^2 + 2x - 2y - 3 = 0$$
 (ii)

(i) of (ii) intersect orthogonally

$$\therefore (2\lambda - 1) + -2\left(\frac{3\lambda}{2} + 1\right) = \lambda - 1 \Longrightarrow \lambda = \frac{-3}{2}$$

Required circle is  $2x^2 + 2y^2 - 10x - 5y + 1 = 0$ 48. Answer (A)

Hint : Touching concept of line with circle.

# Solution :

Let required circle

$$(x^{2} + y^{2} - 4) + \lambda(x + 2y - 4) = 0$$
$$C\left(\frac{-\lambda}{2}, -\lambda\right) = \lambda = \sqrt{\frac{5\lambda^{2}}{4} + 4\lambda + 4}$$

 $\therefore$  it touches line x + 2y - 5 = 0

$$\therefore \left| \frac{\frac{-\lambda}{2} + 2(-\lambda) - 5}{\sqrt{5}} \right| = \sqrt{\frac{5\lambda^2}{4} + 4\lambda + 4}$$

$$\Rightarrow 5(\lambda + 2)^2 = 5\lambda^2 + 16\lambda + 16$$
$$\Rightarrow \lambda = -1$$

- $\therefore$  Required circle  $x^2 + y^2 x 2y = 0$
- 49. Answer (D)

Hint : Chord of contact of circle.

#### Solution :

Equation of C.O.C hx + ky = 8 (i)

Also  $tk = h + 2t^2$  (ii)  $\therefore$  (*h*,*k*) satisfy tangent)

$$\Rightarrow hx + y \frac{(h+2t^2)}{t} - 8 = 0$$
$$\Rightarrow 2(ty-4) + h\left(x + \frac{y}{t}\right) = 0$$

... Line passes through point

$$y = \frac{4}{t}$$
 and  $x = \frac{-y}{t}$ 

 $\Rightarrow \frac{y}{4} = -\frac{x}{y} \Rightarrow y^2 = -4x$ 

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020 Test - 2A (Paper-2) (Code-E)\_(Hints & Solutions)

#### 50. Answer (A)

Hint : Point of intersection of two curves.

#### Solution :

Point of intersection of x = -2 and  $x^2 + y^2 = 16$ 

$$\therefore y^2 = 12 \Rightarrow y = \pm 2\sqrt{3}$$

 $\therefore$  Point $\left(-2, 2\sqrt{3}\right)$ 

51. Answer (C)

Hint : Circumcircle of triangle ABC

### Solution :

The equation of the circumcircle of  $\triangle AQB$  is

 $(x^2 + y^2 - 8) + \lambda(hx + ky - 8) = 0 :: (A = -1)$  due to (0,0) satisfy it

 $\therefore$  Equation is  $x^2 + y^2 - hx - ky = 0$ 

Now centre  $\left(\frac{h}{2}, \frac{k}{2}\right)$ 

 $\therefore$  For locus let  $x = \frac{h}{2}$ ;  $y = \frac{k}{2}$ 

h = 2x and k = 2y

$$\therefore tk = h + 2t^2 \therefore at t = 2$$

The required locus is 2y = x + 4

52. Answer (D)

Hint : Length of latus rectum independency.

Solution :



 $\theta = 2 \tan^{-1} 2$ 

$$\because \sqrt{3} < 2 < \sqrt{2} + 1$$
$$\frac{\pi}{3} < \tan^{-1} 2 < \frac{3\pi}{8}$$

$$\Rightarrow \frac{2\pi}{3} < \theta < \frac{3\pi}{4}$$

53. Answer (B)

**Hint :** Condition of common tangent on two curves.

Solution :

$$y = \frac{x}{2} + 2$$
 is tangent on  $\frac{x^2}{4} + \frac{y^2}{b^2} = 1$ 

 $\Rightarrow 4 + 4b^2 = 16 \Rightarrow b^2 + 1 = 4 \Rightarrow b = \pm\sqrt{3}$ 

Now tangent at other point is given by -2y = x+4

$$\Rightarrow x + 2y + 4 = 0$$

54. Answer (A)

Hint : Locus of midpoint of Parallel chords.

#### Solution :

Let middle point is (*h*,*k*)

... Equation of chord in mid-point form is

$$\frac{x}{h} + \frac{y}{k} = 2$$

$$\therefore -\frac{1}{h \times \frac{1}{k}} = m \Longrightarrow k = -mh$$

 $\Rightarrow$  *y* + *mx* = 0 is the required locus

55. Answer (C)

Hint : I.T.F. conversion in domain.

Solution :

Let  $\sin^{-1}x = \theta \Rightarrow x = \sin \theta$ 

Now

$$\cos^{-1} x = \cos^{-1} \left( \sin \theta \right) = \cos^{-1} \left( -\cos \left( \frac{3\pi}{2} - \theta \right) \right)$$
$$= \pi - \cos^{-1} \left( \cos \left( \frac{3\pi}{2} - \theta \right) \right)$$
$$= \pi - \left( \frac{3\pi}{2} - \theta \right) \text{as } \frac{3\pi}{2} - \theta \in (0, \pi)$$
$$= \theta - \frac{\pi}{2} = \sin^{-1} x - \frac{\pi}{2}$$
$$\therefore \sin^{-1} x + \cos^{-1} x = 2\sin^{-1} x - \frac{\pi}{2}$$

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

56. Answer A(P); B(Q); C(Q, S); D(R, S)

Hint : Type of functions concept.

Solution :

(A) 
$$f(x) = \begin{cases} \left( (1)^{1} \right)^{n} x > 0 = 1 , x > 0 \\ \left( (-1)^{-1} \right)^{n} x < 0 , x < 0 \end{cases}$$

f(x) is an odd function. f(x) is not bijective

 $\therefore$  f(x) is not one one

(B) 
$$f(x) = \frac{x}{e^x - 1} + \frac{x}{2} + 1$$
  
 $f(x) = \frac{-x}{e^{-x} - 1} - \frac{x}{2} + 1 = x + \frac{x}{e^x - 1} - \frac{x}{2} + f(x)$ 

 $\therefore$  f(x) is an even function  $\therefore$  f(x) is not bijective

(C) f(-x) = f(x) : f(x) is even. f(x) is periodic but time period not define

(D)  $f(x) = \max\{\tan x, \cot x\}$ . From graph of f(x) it is clear that

f(x) is neither even nor odd

$$\therefore f(x+\pi) = \max\{\tan(x+\pi), \cot(x+\pi)\}$$

 $= \max \{ \tan x, \cot x \} f(x) \text{ is periodic with } f(x) \text{ is }$ periodic with  $\pi$ 

57. Answer A(P, Q); B(P, Q); C(R, T); D(S, T)

Hint : Property of perpendicular normals.

#### Solution :

Equation of normal at 'p' is

 $y = -tx + 2at + at^3$ 

Put 
$$y = -2at \implies x = 4a + at^2$$

 $\therefore$ G (4a + at<sup>2</sup>, -2at)

Required locus  $y^2 = 4a(x - 4a)$ 

 $\therefore y^2 = 4(x-4)$ 

Now verify each option

58. Answer (09)

Solution :

$$\frac{1}{1-\sin(\cos^{-1}x)} = 2$$
  
$$\Rightarrow \sin(\cos^{-1}x) = \frac{1}{2}$$
  
$$\Rightarrow \cos^{-1}x = \frac{\pi}{6} \Rightarrow x = \frac{\sqrt{3}}{2} \Rightarrow 4x^{2} = 3$$
  
$$\Rightarrow 12x^{2} = 9$$

59. Answer (00)

Hint : Trigonometric conversion of I.T.F.

# Solution :

$$\sin\left(\cos^{-1}\left(\tan\left(\tan^{-1}\left(\sqrt{x^{2}-1}\right)\right)\right)\right)$$
$$= \sin\left(\cos^{-1}\sqrt{x^{2}-1}\right)$$
$$= \sin\left(\sin^{-1}\sqrt{2-x^{2}}\right) = \sqrt{2-x^{2}}$$
$$\therefore \text{ Common domain } \left[1,\sqrt{2}\right] \Rightarrow 2-x^{2} = 1+x$$

$$\Rightarrow x^{2} + x - 1 = 0 \Rightarrow x = \frac{-1 \pm \sqrt{5}}{2}$$
$$x = \frac{\sqrt{5} - 1}{2} \notin \left[1, \sqrt{2}\right]$$

∴ No solution exists

2

60. Answer (03)

Hint : Graphical solution.

Solution :



From graph it is clear that curves intersect at 3 points

.: Only 3 solutions

# All India Aakash Test Series for JEE (Advanced)-2020

# TEST - 2A (Paper-2) - Code-F

Test Date : 24/11/2019

# ANSWERS

| PHYSICS |                        | СН  | CHEMISTRY        |     | MATHEMATICS            |  |
|---------|------------------------|-----|------------------|-----|------------------------|--|
| 1.      | (A)                    | 21. | (C, D)           | 41. | (B, C)                 |  |
| 2.      | (B, C)                 | 22. | (A, C, D)        | 42. | (A, B)                 |  |
| 3.      | (A, D)                 | 23. | (D)              | 43. | (A)                    |  |
| 4.      | (B, D)                 | 24. | (A, C, D)        | 44. | (B, D)                 |  |
| 5.      | (B, D)                 | 25. | (B, C, D)        | 45. | (B, C)                 |  |
| 6.      | (D)                    | 26. | (D)              | 46. | (C)                    |  |
| 7.      | (B)                    | 27. | (B)              | 47. | (D)                    |  |
| 8.      | (C)                    | 28. | (A)              | 48. | (A)                    |  |
| 9.      | (A)                    | 29. | (B)              | 49. | (D)                    |  |
| 10.     | (C)                    | 30. | (A)              | 50. | (A)                    |  |
| 11.     | (C)                    | 31. | (B)              | 51. | (C)                    |  |
| 12.     | (A)                    | 32. | (A)              | 52. | (C)                    |  |
| 13.     | (B)                    | 33. | (C)              | 53. | (A)                    |  |
| 14.     | (C)                    | 34. | (B)              | 54. | (B)                    |  |
| 15.     | (B)                    | 35. | (A)              | 55. | (D)                    |  |
| 16.     | $A \rightarrow (R, T)$ | 36. | $A \to (Q,S)$    | 56. | $A \rightarrow (P, Q)$ |  |
|         | $B \rightarrow (S, T)$ |     | $B \to (Q)$      |     | $B \to (P,Q)$          |  |
|         | $C \rightarrow (Q, S)$ |     | $C \to (R,T)$    |     | $C \to (R,T)$          |  |
|         | $D \rightarrow (Q, S)$ |     | $D \to (Q)$      |     | $D\to(S,T)$            |  |
| 17.     | $A \rightarrow (P, R)$ | 37. | $A \to (Q,S)$    | 57. | $A \rightarrow (P)$    |  |
|         | $B \rightarrow (P, S)$ |     | B  ightarrow (R) |     | $B \to (Q)$            |  |
|         | $C \rightarrow (Q, T)$ |     | $C \to (Q,R)$    |     | $C \to (Q,S)$          |  |
|         | $D \rightarrow (Q, S)$ |     | $D\to(P,T)$      |     | $D \to (R,S)$          |  |
| 18.     | (06)                   | 38. | (06)             | 58. | (03)                   |  |
| 19.     | (01)                   | 39. | (03)             | 59. | (00)                   |  |
| 20.     | (02)                   | 40. | (07)             | 60. | (09)                   |  |

# **HINTS & SOLUTIONS**

# **PART - I (PHYSICS)**

1. Answer (A)

Hint : A balanced wheatstone bridge is formed. Solution :

$$\therefore V_D - V_C = 0$$
  
$$\therefore R_{eq} = \frac{12 \times 6}{12 + 6} = 4 \Omega$$
  
$$\therefore I_{battery} = \frac{20}{4} = 5 A$$

$$I_{AD} = \frac{20}{12} = \frac{5}{3} A$$

2. Answer (B, C)

**Hint** :  $\Delta Q = \Delta U + \Delta W$ 

# Solution :

$$Q = \Delta U + \frac{Q}{2} \implies \Delta U = \frac{Q}{2}$$
$$\implies n \times \left(\frac{3R}{2}\right) \cdot \Delta T = \frac{nC\Delta T}{2}$$
$$\implies C = 3R$$
And,  $\Delta U = \Delta W$ 

$$\Rightarrow n\left(\frac{3R}{2}\right) \cdot dT = PdV$$

- $\Rightarrow P^3V = \text{constant}$
- $\Rightarrow P^2 \times T = \text{constant}$

$$\Rightarrow P \propto \frac{1}{\sqrt{T}}$$

3. Answer (A, D)

Hint : Frequency as well as wavelength change. Solution :

$$\lambda_{1} = \lambda_{0} - \frac{V}{5}T \implies \lambda_{1} = \frac{4\lambda_{0}}{5}$$
$$\therefore \quad \lambda_{2} = 2\lambda_{1} = \frac{8\lambda_{0}}{5}$$
and, 
$$T' = \frac{\lambda'}{2V + \frac{V}{5}} = \frac{5\lambda'}{11V}$$
$$\therefore \quad f' = \frac{1}{T'} = \frac{11V}{5 \times \left(\frac{8\lambda_{0}}{5}\right)} = \frac{11V}{8f_{0}}$$

4. Answer (B, D) Hint : Particle performs SHM. Solution :

$$E = \frac{Qx}{4\pi\varepsilon_0 (R^2 + x^2)^{\frac{3}{2}}}, \quad x \ll R$$
  

$$\Rightarrow \quad E = \frac{Qx}{4\pi\varepsilon_0 R^3}$$
  

$$\therefore \quad \omega = \sqrt{\frac{Qq}{m \times 4\pi\varepsilon_0 R^3}}$$
  

$$\therefore \quad T = 2\pi \sqrt{\frac{m \times 4\pi\varepsilon_0 R^3}{Qq}} = 4\pi \sqrt{\frac{\pi\varepsilon_0 m R^3}{Qq}}$$
  
and,  $V_{max} = \omega a = \frac{ax}{2} \sqrt{\frac{Qq}{\pi\varepsilon_0 m R^3}}$ 

5. Answer (B, D)

Hint : *B* and *C* will be in series. Solution :

$$C_{BC} = \frac{2 \times 3}{2 + 3} = \frac{6}{5} \mu F$$
  
$$\therefore \quad \Delta q_S = \frac{\frac{6}{5}}{\frac{6}{5} + 1} \times 110 = 60 \ \mu C$$
  
$$\therefore \quad q_A = 110 - 60 = 50 \ \mu C$$

$$V_B = \frac{60}{2} = 30 \text{ V}, \ V_C = \frac{60}{3} = 20 \text{ V}$$

6. Answer (D)

Hint : Two spheres behave as capacitor and then become in parallel finally.

#### Solution :

 $\sim$ 

$$Q_{0} = 4\pi\varepsilon_{0} (2a) \times V$$
  

$$\therefore \quad i = \frac{V}{R} e^{-\frac{t}{\tau}}, \quad \tau = R \times \left(\frac{C_{1}C_{2}}{C_{1} + C_{2}}\right)$$
  

$$= R \times \frac{4\pi\varepsilon_{0}a \times 2a}{3a}$$
  

$$= \frac{8\pi\varepsilon_{0}Ra}{3}$$
  

$$\therefore \quad i = \frac{V}{R} e^{-\frac{3t}{8\pi\varepsilon_{0}Ra}}$$

7. Answer (B)

Hint : Two spheres behave as capacitor and then become in parallel finally.

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

## Solution :

Final charge on smaller sphere

$$q_{2} = \frac{C_{2}}{C_{1} + C_{2}} \times Q_{0}$$
$$= \frac{4\pi\varepsilon_{0} \times a}{4\pi\varepsilon_{0} (a + 2a)} \times \left[4\pi\varepsilon_{0} \times (2a) \times V\right]$$
$$= \frac{1}{3} \times 8\pi\varepsilon_{0} aV$$

8. Answer (C)

**Hint :** Two spheres behave as capacitor and then become in parallel finally.

#### Solution :

Total heat dissipation

$$H = \frac{1}{2} \times \left(\frac{C_1 C_2}{C_1 + C_2}\right) \times V^2$$
$$= \frac{1}{2} \times \frac{2}{3} \times (4\pi\varepsilon_0 a) V^2$$
$$= \frac{4\pi\varepsilon_0 a V^2}{3}$$

9. Answer (A)

**Hint :** Speed of sound,  $V = \sqrt{\frac{\gamma RT}{M}}$ 

Solution :

$$V = \sqrt{\frac{\gamma RT}{M}}$$
  

$$\Rightarrow T = \frac{V^2 M}{\gamma R} = \frac{(300)^2 \times (29 \times 10^{-3})}{1.4 \times 8.314}$$
  

$$\approx 224 \text{ K}$$

- 10. Answer (C)Hint : Put the value of *T*<sub>0</sub>.Solution :
  - $:: T = T_0 0.006 h_0$
  - $\Rightarrow$  273 = 224 0.006 ×  $h_0$

$$\Rightarrow$$
  $h_0 = 8170 \text{ m}$ 

11. Answer (C)

**Hint :** Put the value of  $h_0$ . **Solution :** 

$$P = P_0 \left( 1 - \frac{0.006 \times 8170}{273} \right) \frac{29 \times 10^{-3} \times 9.8}{8.31 \times 0.006}$$
  
=  $P_0 \times (0.82)^{5.7}$   
=  $0.32 P_0$   
12. Answer (A)  
Hint :  $P^{1-\gamma} T^{\gamma}$  = constant  
Solution :

$$P_1^{1-\gamma}T_1^{\gamma}=P_2^{1-\gamma}T_2^{\gamma}$$

$$\Rightarrow T_2 = 1000 \times \left(\frac{3}{2}\right)^{\left(\frac{3}{5}-1\right)} = 850 \text{ K}$$
  
Then,  $\frac{P_3}{T_3} = \frac{P_2}{T_2} \Rightarrow T_3 = 425 \text{ K}$   
 $\therefore \Delta Q = nC_v \Delta T = 1 \times \left(\frac{3R}{2}\right) \times (850 - 425)$   
 $= 5300 \text{ J}$ 

13. Answer (B)Hint : Use concept of standing wave.Solution :

$$y = y_1 + y_2$$

$$= a \left[ \sin \left( \frac{\pi}{2} x - \omega t \right) + \sin \left( \frac{\pi}{2} x + \omega t + \frac{\pi}{3} \right) \right]$$

$$\Rightarrow \quad y = 2a \sin \left( \frac{\pi}{2} x + \frac{\pi}{6} \right) \cdot \cos \left( \cot + \frac{\pi}{6} \right)$$
For nodes,  $2a \sin \left( \frac{\pi}{2} x + \frac{\pi}{6} \right) = 0$ 

$$\Rightarrow \quad \frac{\pi}{2} x + \frac{\pi}{6} = \pi, 2\pi, 3\pi, 4\pi, ....$$

$$\Rightarrow \quad x = \frac{5}{3}, \frac{11}{3}, \frac{17}{3}, \frac{23}{3}$$

$$\therefore \quad \text{For } 0 \le x \le 6,$$
Number of nodes = 3
14. Answer (C)
Hint : Flux =  $\frac{q}{4\pi\varepsilon_0} \times \text{Solid angle} \times 2$ 

Solution :

$$\phi = \frac{q}{\varepsilon_0} \times \frac{2\pi(1 - \cos\theta)}{4\pi} \times 2$$
$$= \frac{q}{\varepsilon_0} \left( 1 - \frac{\ell}{\sqrt{\ell^2 + R^2}} \right) = \frac{q}{\varepsilon_0} \left( 1 - \frac{2}{\sqrt{5}} \right)$$

15. Answer (B) Hint : Use KVL and KCL Solution :



*:*..



Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020 Test - 2A (Paper-2) (Code-F)\_(Hints & Solutions)

For R<sub>AC</sub>



$$\therefore \quad R_{AC} = \frac{3R}{4}$$
$$\therefore \quad \frac{R_{AB}}{R_{AC}} = \frac{7 \times 4}{12 \times 3} = \frac{7}{9}$$

- 16. Answer A(R, T); B(S, T); C(Q, S); D(Q, S) Hint : In isothermal process  $\Delta U = 0$ Solution :
  - For A : PV = constant
  - $\Rightarrow \Delta U = 0, \Delta W = \text{positive}$

$$\Rightarrow \Delta Q = \text{positive}$$

For B : 
$$P = \frac{pRT}{m} \Rightarrow T = \text{constant}$$

$$\Rightarrow \Delta U = 0, \Delta W = -\text{negative}, \Delta Q = \text{negative}$$
  
And so on.

Answer A(P, R); B(P, S); C(Q, T); D(Q, S)
 Hint : After earthing, charge on outer surface of outer most plates becomes zero.

# Solution :

Before earthing



18. Answer (06)

Hint : Use superposition principle. Solution :

$$E_1 = \frac{Q}{4\pi\varepsilon_0 a^2}$$



19. Answer (01)

Hint : Use Newton's law.

$$\frac{-dT}{dt} = b(T - T_s)$$

$$\Rightarrow \Delta T = (\Delta T)_0 e^{-bt}$$

$$\therefore t_2 = 2t_0$$

$$\therefore n = 1$$

20. Answer (02)

Hint : Reduce it to a finite circuit. Solution :

$$R_{AB} = R_{CD}, \ V_{CD} = \frac{1}{2} V_{AB}$$

... Current gets equally distributed

$$\therefore R_2 = R_{AB}$$

And, 
$$R_{AB} = R_1 + \left(\frac{R_2}{2}\right) = R_2$$

$$\Rightarrow \frac{R_2}{R_1} = 2$$

# PART - II (CHEMISTRY)

SO.F

21. Answer (C, D) Hint : P is







22. Answer (A, C, D)



is more basic than aniline

#### Solution :



are less basic than aniline

23. Answer (D)



#### Solution :



24. Answer (A, C, D)

Hint :



### Solution :

Q is slightly basic

P contains fluorine atom

Because of the presence of  $-NH_2$  group, Q can give coupling reaction

#### 25. Answer (B, C, D)

**Hint :** Benzaldehyde is not oxidised by Fehling's reagent.

# Solution :

Acetophenone can give iodoform and bromoform.

26. Answer (D)

Hint : Given D-glyceraldehyde is 'R'



Solution :



R as well as D.

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020

# Test - 2A (Paper-2) (Code-F)\_(Hints & Solutions)

#### 27. Answer (B)

Hint : D and L convention is used for amino acids also

# Solution :

- (D) fructose is laevorotatory (I)
- (D) glucose is dextrorotatory(d)
- 28. Answer (A)

Hint : Product obtained after ozonolysis

$$H_{3}CO \xrightarrow{H}_{CH_{3}}CH O = C \xrightarrow{H}_{CH_{3}}CH_{3} \xrightarrow{H}_{CH_{3}}OCH_{3}$$

- Solution :
- C\* is L

C<sup>#</sup> is D.

- 29. Answer (B)
- 30. Answer (A)
- 31. Answer (B)

# Hint and Solution : Q. Nos. 29 to 31







32. Answer (A)

Hint : Excess of ether and water as solvent will favour  $S_N 1$  reaction.

### Solution :



33. Answer (C)

Hint :



Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

#### Solution :









Solution :



35. Answer (A)

Hint : It is electrophilic substitution reaction.

# Solution :

The intermediate formed when  ${}^{+}NO_{2}$  attacks at position C-2 is more stable.

36. Answer A(Q, S); B(Q); C(R, T); D(Q)

**Hint :** LiAIH<sub>4</sub> is a very strong reducing agent can reduce almost functional groups to lower oxidation state, except alkenes and alkynes.

# Solution :

NaBH<sub>4</sub> cannot reduce amide into amine

NaBH<sub>4</sub> can reduce only acid halide into alcohol among the given transformation.

37. Answer A(Q, S); B(R); C(Q, R); D(P, T)

# Hint :



Solution :



38. Answer (06)

**Hint :** O, P-substituted Bromo group are more likely to get substituted.

# Solution :

The Br group at position 4 is most likely to get substitute and at position 2, is least

39. Answer (03)

Hint :



Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020 Test - 2A (Paper-2) (Code-F)\_(Hints & Solutions)

#### Solution :

Possible Products

40. Answer (07)

Hint : 
$$5 \xrightarrow{6} 1 CI$$
  
 $O_2N \xrightarrow{4} 0 \xrightarrow{3} 2 NO_2$ 

Solution :

x = 1, y = 2, z = 4

# PART - III (MATHEMATICS)

41. Answer (B, C)

Hint : Perpendicularity of two lines.

# Solution :

 $L_1$  and  $L_2$  if they are  $\perp$  to a common line  $\Rightarrow \lambda = -1$  for two adjacent sides of a square

 $L_1 \perp L_2$ 

$$\therefore (\lambda^2 + 1) \lambda^2 = 1$$

$$\Rightarrow \lambda^5 + 2\lambda^3 + \lambda - 1 = 0 = f(\lambda)$$

$$\therefore f'(\lambda) = 5\lambda^4 + 6\lambda^2 + 1 = 0$$

 $\therefore$   $f(\lambda) = 0$  has only one real root

42. Answer (A, B)

**Hint :** Condition of two degree equation (to represent pair of straight line.

#### Solution :

$$\Delta = 0 \Longrightarrow abc + 2fgh = af^2 + bg^2 + ch^2$$

$$\Rightarrow c = \frac{-10}{9}$$

Also

$$\cos \alpha = \left| \frac{a+b}{\sqrt{\left(a-b\right)^2 + 4h^2}} \right| \Rightarrow \alpha = \cos^{-1}\left(\frac{5}{\sqrt{34}}\right)$$

43. Answer (A)

Hint : Division formula between two points.

Solution :

$$A\left(\frac{ab}{a+b}\left(\frac{1-m}{-m},0\right):B\left(-0,\frac{ab}{a+b}\left(1-m\right)\right)\right)$$

Mid-point of AB is (h, k)

$$\therefore 2h = \frac{ab}{a+b} \frac{(m-1)}{m}; 2k \frac{ab}{a+b} (1-m)$$

$$\therefore \frac{1}{2h} + \frac{1}{2k} = \frac{a+b}{ab}$$

 $\Rightarrow$  ab (x + y) = 2 (a + b) xy is the locus

Let P divides AB in ratio 1:3

$$\therefore P\left(\frac{\frac{3ab}{a+b}\left(1-\frac{1}{m}\right)}{4}, \frac{\frac{ab}{a+b}\left(1-m\right)}{4}\right)$$

 $\therefore$  (*x* + 3*y*)*ab* = 4(*a* + *b*)*xy* is the required locus

44. Answer (B, D)

Hint : Distance between two parallel lines.

# Solution :

Distance between two parallel lines =  $2\sqrt{5}$ 

$$\therefore \text{ points on line } \frac{x-1}{\frac{-2}{\sqrt{5}}} = \frac{y+2}{\frac{1}{\sqrt{5}}} = \pm 2\sqrt{5}$$

- $\therefore$  points are (-3, 0) and (5, -4)
- ... Required lines are

$$2x - y + 6 = 0$$
 and  $2x - y - 14 = 0$ 

45. Answer (B, C)

Hint : Translation and Rotation of axes.

#### Solution :

For 
$$f(x,y) = 0$$

new origin=

$$\left(\frac{hf-bh}{ab-h^2},\frac{gf-af}{ab-h^2}\right) \equiv \left(\frac{28}{-14},\frac{42}{-14}\right) \equiv \left(-2,-3\right)$$

For 
$$g(x,y) = 0$$

$$\theta = \frac{1}{2} \tan^{-1} \left( \frac{2h}{a-b} \right) = \frac{1}{2} \tan^{-1} \left( \frac{2 \times \sqrt{3}}{2} \right)$$

$$=\frac{1}{2}\times\frac{\pi}{3}=\frac{\pi}{6}$$

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

#### 46. Answer (C)

Hint : Family of circle with line.

## Solution :

Let required circle

$$x^2 + y^2 - 3x + 2y - 4 + \lambda (2x + 5y + 2) = 0$$

$$\therefore C\left(\frac{3-2\lambda}{2}, \frac{-(5\lambda+2)}{2}\right) \text{ satisfy } x+y=11$$

$$\lambda = -3$$

- $\therefore$  Required circle is  $x^2 + y^2 9x 13y 10 = 0$
- 47. Answer (D)

Hint : Orthogonal of two circles.

#### Solution :

Let required circle

 $(x-1)^2 + (y+1)^2 + \lambda(2x+3y+1) = 0$  (i)

Circle with diameter points (0,3) and (-2,-1) is

$$x^2 + y^2 + 2x - 2y - 3 = 0$$
 (ii)

(i) of (ii) intersect orthogonally

$$\therefore \left(2\lambda - 1\right) + -2\left(\frac{3\lambda}{2} + 1\right) = \lambda - 1 \Longrightarrow \lambda = \frac{-3}{2}$$

Required circle is  $2x^2 + 2y^2 - 10x - 5y + 1 = 0$ 48. Answer (A)

Hint : Touching concept of line with circle.

#### Solution :

Let required circle

$$(x^{2} + y^{2} - 4) + \lambda(x + 2y - 4) = 0$$
$$C\left(\frac{-\lambda}{2}, -\lambda\right) = \lambda = \sqrt{\frac{5\lambda^{2}}{4} + 4\lambda + 4}$$

 $\therefore$  it touches line x + 2y - 5 = 0

$$\therefore \left| \frac{\frac{-\lambda}{2} + 2(-\lambda) - 5}{\sqrt{5}} \right| = \sqrt{\frac{5\lambda^2}{4} + 4\lambda + 4}$$

$$\Rightarrow 5(\lambda + 2)^2 = 5\lambda^2 + 16\lambda + 16$$
$$\Rightarrow \lambda = -1$$

$$\therefore \text{ Required circle } x^2 + y^2 - x - 2y = 0$$

49. Answer (D)

Hint : Chord of contact of circle.

# Solution :

Equation of C.O.C hx + ky = 8 (i) Also  $tk = h + 2t^2$  (ii)  $\because (h,k)$  satisfy tangent)

$$\Rightarrow hx + y \frac{(h+2t^2)}{t} - 8 = 0$$
$$\Rightarrow 2(ty-4) + h\left(x + \frac{y}{t}\right) = 0$$

 $\therefore \text{ Line passes through point} \\ y = \frac{4}{t} \text{ and } x = \frac{-y}{t}$ 

$$\Rightarrow \frac{y}{4} = -\frac{x}{y} \Rightarrow y^2 = -4x$$

50. Answer (A)

Hint : Point of intersection of two curves.

#### Solution :

Point of intersection of x = -2 and  $x^2 + y^2 = 16$ 

$$\therefore y^2 = 12 \Rightarrow y = \pm 2\sqrt{3}$$
$$\therefore \text{Point}\left(-2, 2\sqrt{3}\right)$$

51. Answer (C)

Hint : Circumcircle of triangle ABC

# Solution :

The equation of the circumcircle of  $\triangle AQB$  is

 $(x^2 + y^2 - 8) + \lambda(hx + ky - 8) = 0 :: (A = -1)$  due to (0,0) satisfy it

 $\therefore$  Equation is  $x^2 + y^2 - hx - ky = 0$ 

Now centre  $\left(\frac{h}{2}, \frac{k}{2}\right)$ 

$$\therefore$$
 For locus let  $x = \frac{h}{2}; y = \frac{k}{2}$ 

$$h = 2x$$
 and  $k = 2y$ 

 $\therefore$   $tk = h + 2t^2$   $\therefore$  at t = 2

The required locus is 2y = x + 4

52. Answer (C)

# Hint : I.T.F. conversion in domain.

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

# All India Aakash Test Series for JEE (Advanced)-2020 Test - 2A (Paper-2) (Code-F)\_(Hints & Solutions)

#### Solution :

Let 
$$\sin^{-1}x = \theta \Rightarrow x = \sin \theta$$

Now

$$\cos^{-1} x = \cos^{-1} \left( \sin \theta \right) = \cos^{-1} \left( -\cos \left( \frac{3\pi}{2} - \theta \right) \right)$$
$$= \pi - \cos^{-1} \left( \cos \left( \frac{3\pi}{2} - \theta \right) \right)$$
$$= \pi - \left( \frac{3\pi}{2} - \theta \right) \text{as } \frac{3\pi}{2} - \theta \in (0, \pi)$$
$$= \theta - \frac{\pi}{2} = \sin^{-1} x - \frac{\pi}{2}$$
$$\therefore \sin^{-1} x + \cos^{-1} x = 2\sin^{-1} x - \frac{\pi}{2}$$

53. Answer (A)

Hint : Locus of midpoint of Parallel chords.

#### Solution :

Let middle point is (h,k)

... Equation of chord in mid-point form is

$$\frac{x}{h} + \frac{y}{k} = 2$$
$$\therefore -\frac{1}{h \times \frac{1}{k}} = m \Longrightarrow k = -mh$$

 $\Rightarrow$  *y* + *mx* = 0 is the required locus

#### 54. Answer (B)

**Hint :** Condition of common tangent on two curves.

#### Solution :

$$y = \frac{x}{2} + 2$$
 is tangent on  $\frac{x^2}{4} + \frac{y^2}{b^2} = 1$ 

$$\Rightarrow 4 + 4b^2 = 16 \Rightarrow b^2 + 1 = 4 \Rightarrow b = \pm\sqrt{3}$$

Now tangent at other point is given by -2y = x+4

$$\Rightarrow x + 2y + 4 = 0$$

55. Answer (D)

Hint : Length of latus rectum independency.



56. Answer A(P, Q); B(P, Q); C(R, T); D(S, T) **Hint** : Property of perpendicular normals. **Solution** : Equation of normal at 'p' is  $y = -tx + 2at + at^{3}$ Put  $y = -2at \Rightarrow x = 4a + at^{2}$   $\therefore$  G (4a + at<sup>2</sup>, -2at) Required locus  $y^{2} = 4a (x - 4a)$  $\therefore a = 1$ 

 $\therefore y^2 = 4(x - 4)$ Now verify each option

57. Answer A(P); B(Q); C(Q, S); D(R, S)Hint : Type of functions concept.Solution :

(A) 
$$f(x) = \begin{cases} \left( (1)^{1} \right)^{n} x > 0 = 1 , x > 0 \\ \left( (-1)^{-1} \right)^{n} x < 0 , x < 0 \end{cases}$$

f(x) is an odd function. f(x) is not bijective

 $\therefore$  f(x) is not one one

(B) 
$$f(x) = \frac{x}{e^x - 1} + \frac{x}{2} + 1$$

$$f(x) = \frac{-x}{e^{-x} - 1} - \frac{x}{2} + 1 = x + \frac{x}{e^{x} - 1} - \frac{x}{2} + f(x)$$

 $\therefore$  f(x) is an even function  $\therefore$  f(x) is not bijective

(C)  $f(-x) = f(x) \therefore f(x)$  is even. f(x) is periodic but time period not define

(D)  $f(x) = \max\{\tan x, \cot x\}$ . From graph of f(x) it is clear that

f(x) is neither even nor odd

Aakash Educational Services Limited - Regd. Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 Ph.011-47623456

$$\therefore f(x+\pi) = \max\{\tan(x+\pi), \cot(x+\pi)\}$$

 $= \max \{ \tan x, \cot x \} f(x) \text{ is periodic with } f(x) \text{ is } periodic with } \pi$ 

Hint : Graphical solution.

Solution :



From graph it is clear that curves intersect at 3 points

- .: Only 3 solutions
- 59. Answer (00)

Hint : Trigonometric conversion of I.T.F.

# Solution :

$$\sin\left(\cos^{-1}\left(\tan\left(\tan^{-1}\left(\sqrt{x^{2}-1}\right)\right)\right)\right)$$
$$=\sin\left(\cos^{-1}\sqrt{x^{2}-1}\right)$$

$$= \sin\left(\sin^{-1}\sqrt{2-x^2}\right) = \sqrt{2-x^2}$$
  

$$\therefore \text{ Common domain } \left[1,\sqrt{2}\right] \Rightarrow 2-x^2 = 1$$
  

$$\Rightarrow x^2 + x - 1 = 0 \Rightarrow x = \frac{-1 \pm \sqrt{5}}{2}$$
  

$$x = \frac{\sqrt{5}-1}{2} \notin \left[1,\sqrt{2}\right]$$

+ **X** 

.: No solution exists

60. Answer (09)

Hint : Sum of infinite G.P. Solution :

$$\frac{1}{1-\sin(\cos^{-1}x)} = 2$$
  
$$\Rightarrow \sin(\cos^{-1}x) = \frac{1}{2}$$
  
$$\Rightarrow \cos^{-1}x = \frac{\pi}{6} \Rightarrow x = \frac{\sqrt{3}}{2} \Rightarrow 4x^{2} = 3$$
  
$$\Rightarrow 12x^{2} = 9$$

